Intervention for Algebra I Module 1: Teacher Masters











Mathematics Institute for Learning Disabilities and Difficulties

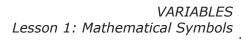
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E ngage Prior Knowledge Practice

Brainstorm

List symbols that are used in mathematics.

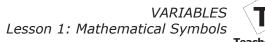


E ngage Prior Knowledge Practice Key

Brainstorm

List symbols that are used in mathematics.

Н	F	-	_		×	÷.
					•	/
					*	<u>1</u> 2
					()	
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				()2	
Other pos	ssible sym	bols:				
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Demonstration Practice

Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

1. 1	g = 1,000 m	g		
	Example	or	Nonexample	
	Because			
2. 3	x-1=y			
	Example	or	Nonexample	
	Because			
3.	a	3		
	-		Nonexample	
4.	3 cm 5 4 cm	cm		
	Example	or	Nonexample	
	Because			



D emonstration Practice Key

Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

1. 1 g = 1,000 mg				
Example or Nonexample				
Because "g" and "mg" are abbreviations for units of measure				
2. $3x - 1 = y$				
Example or Nonexample				
Because "x" and "y" represent a set of values				
3 . 3				
Example or Nonexample				
Because "a" represents the value of the length of 1 side				
4. 3 cm 5 cm 4 cm				
Example or Nonexample				
Because "cm" is an abbreviation for a unit of measure				



P ractice

Activity 1: Guided Practice

Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.

	3 ³ ≥ 25		
	Example	or	Nonexample
		re are	no symbols that represent 1 value or set of
	values		
1.	5 m = 500 cm		
	Example	or	Nonexample
	Because		
2.	N		
	P	R	
	Example	or	Nonexample
	Because		
3.	$V = \frac{100}{p}$		
	Example	or	Nonexample
	Because		



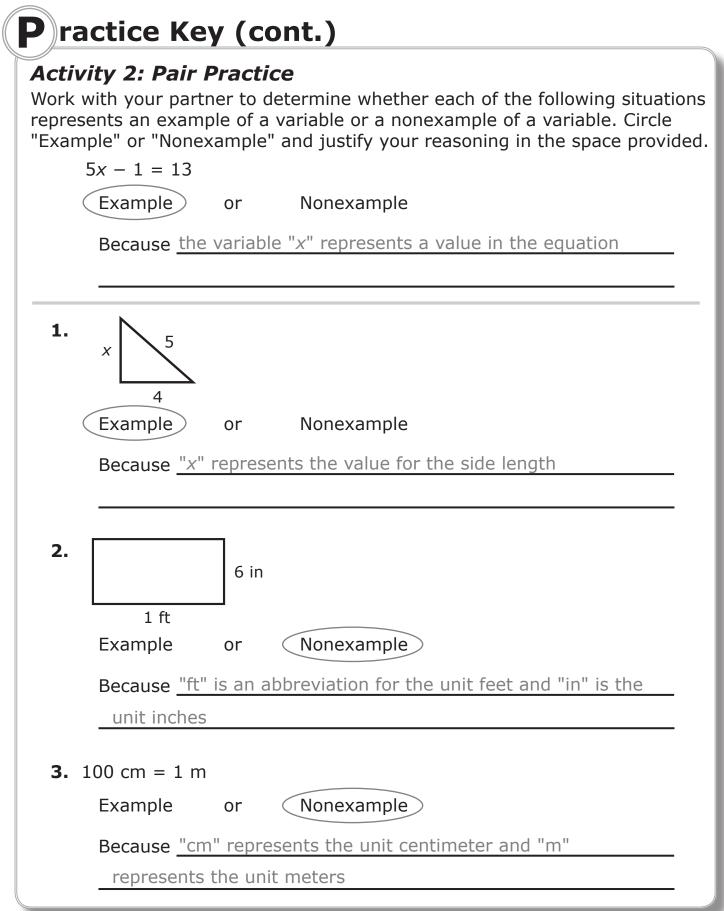
Practice (cont.)
Activity 2: Pair Practice Work with your partner to determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided $5x - 1 = 13$
Example or Nonexample
Because the variable "x" represents 1 value in the equation
1. $x = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$
Example or Nonexample
Because
2. 6 in
1 ft Example or Nonexample
Because
3. $100 \text{ cm} = 1 \text{ m}$
Example or Nonexample
Because



Practice Key
Activity 1: Guided Practice Determine whether each of the following situations represents an example of a variable or a nonexample of a variable. Circle "Example" or "Nonexample" and justify your reasoning in the space provided.
$3^3 \ge 25$
Example or Nonexample
Because there are no symbols that represent a value or set of values
1. 5 m = 500 cm
Example or Nonexample
Because <u>"m" and "cm" are units that label the numbers as 5</u> meters and 500 centimeters
$\begin{array}{c} 2. & N \\ P & \frown & R \end{array}$
Example or Nonexample
Because <u>"A," "B," and "C" label the vertices, or corners, of the</u> triangle
3. $V = \frac{100}{p}$ Example or Nonexample
Because <u>"V" and "p" represent a set of unknown values</u>

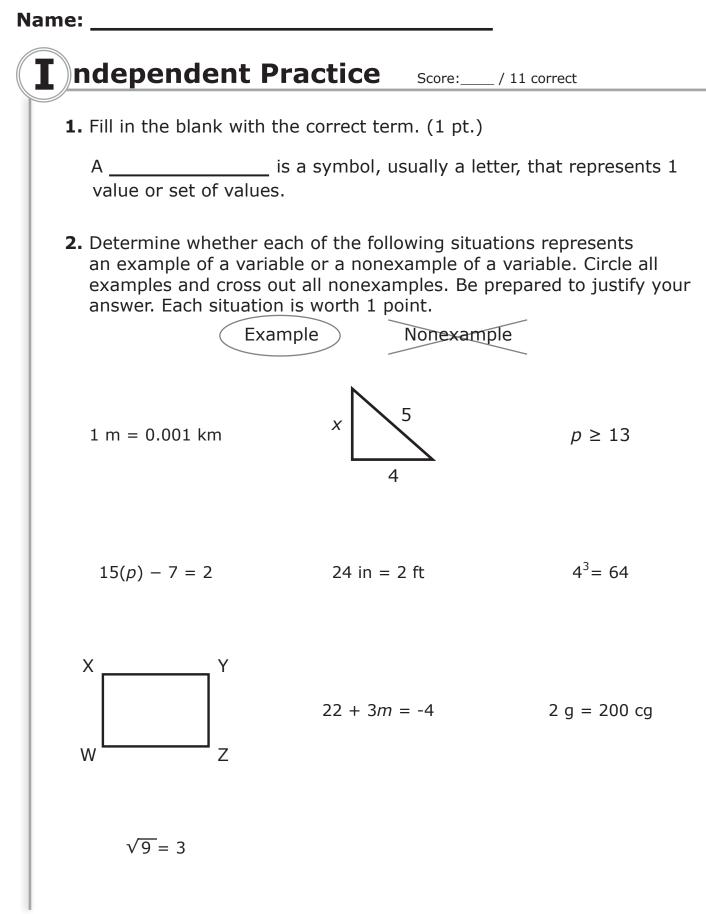
VARIABLES Lesson 1: Mathematical Symbols

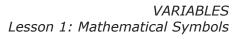




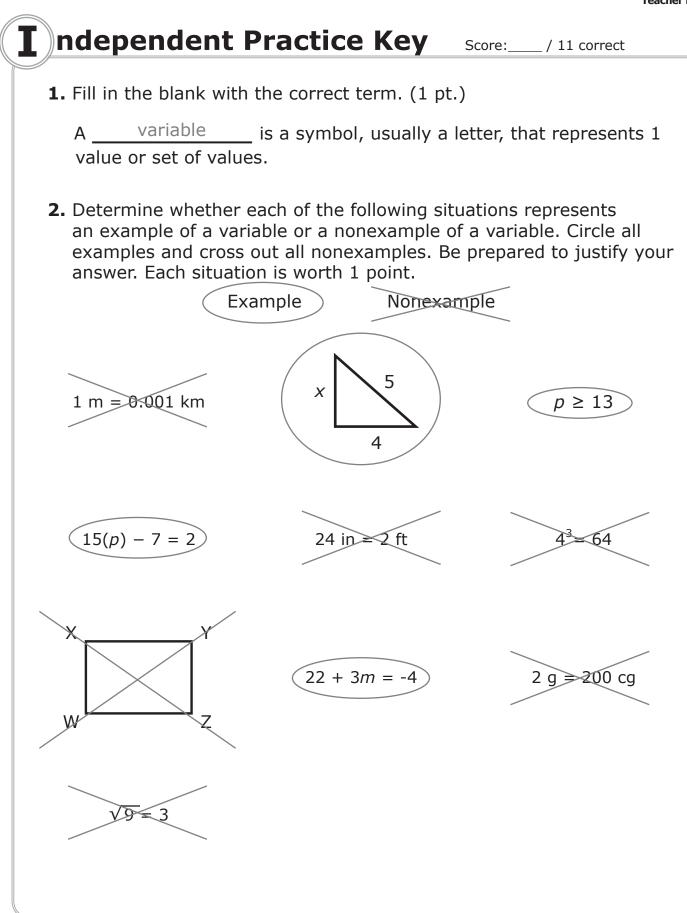
VARIABLES Lesson 1: Mathematical Symbols



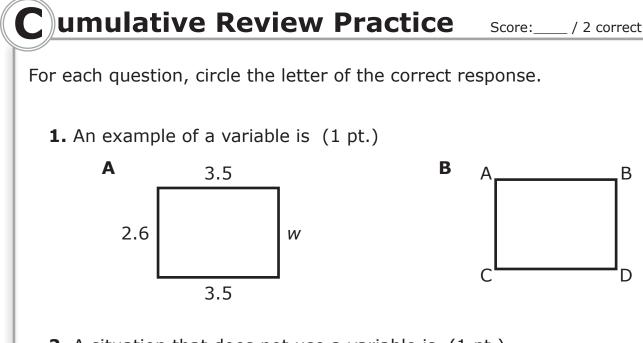




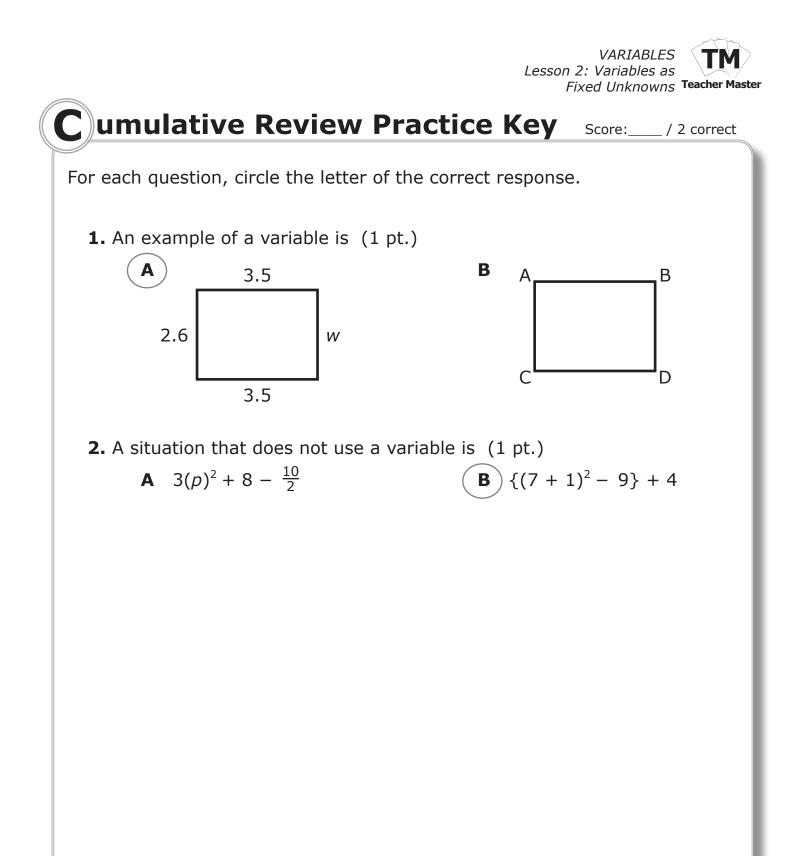




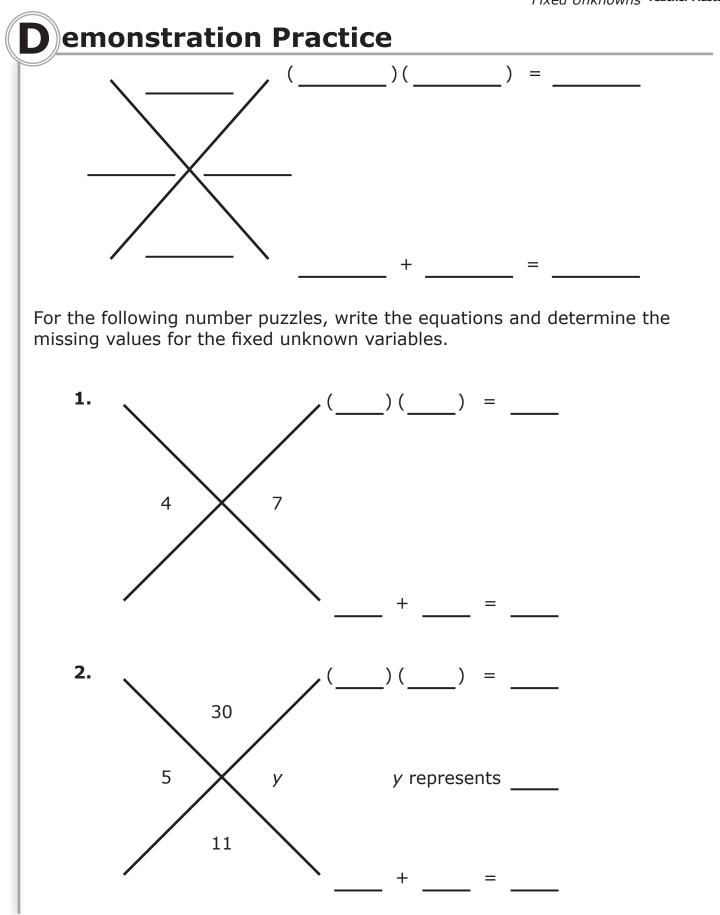


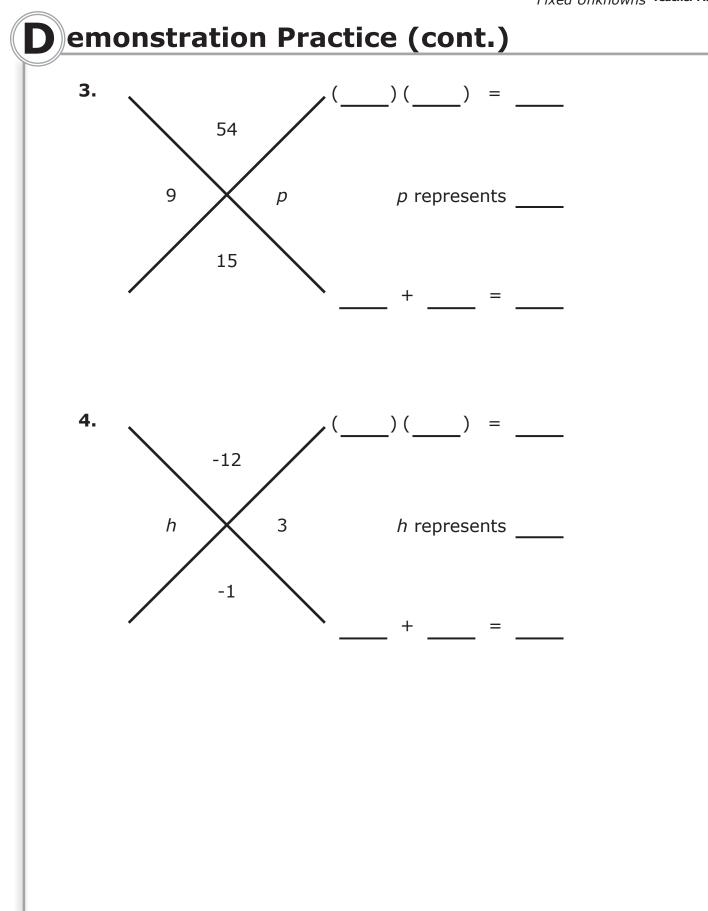


- **2.** A situation that does not use a variable is (1 pt.)
 - **A** $3(p)^2 + 8 \frac{10}{2}$ **B** $\{(7+1)^2 9\} + 4$

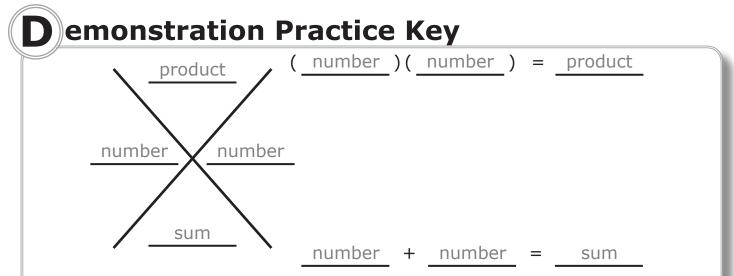


VARIABLES Lesson 2: Variables as Fixed Unknowns Teacher Master

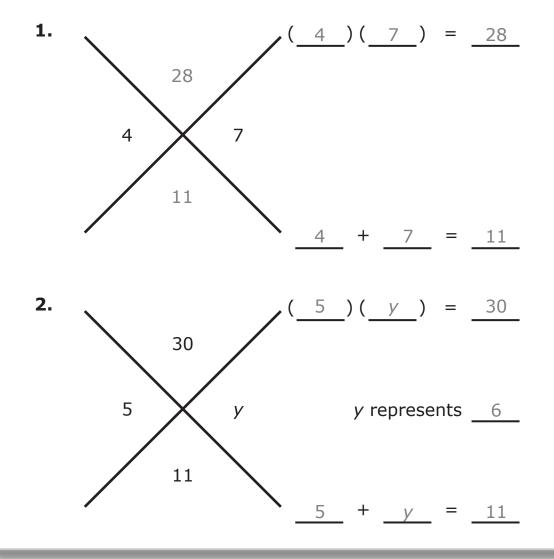




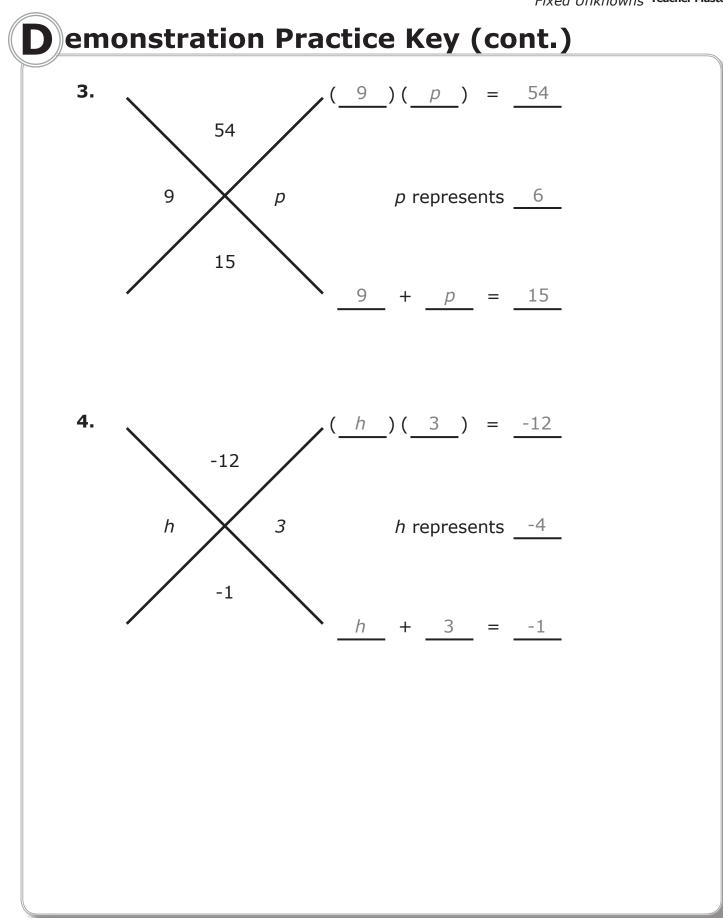
VARIABLES Lesson 2: Variables as Fixed Unknowns



For the following number puzzles, write the equations and determine the missing values for the fixed unknown variables.



VARIABLES Lesson 2: Variables as Fixed Unknowns Teacher Master



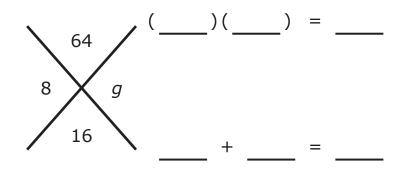


P ractice

Pair Practice

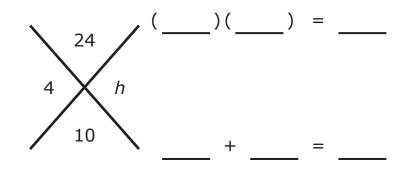
With your partner, for each of the following number puzzles, determine what the fixed unknown variable represents.

1. Determine the value for the variable that is a fixed unknown.



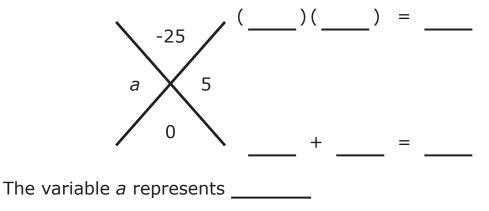
The variable g represents _____

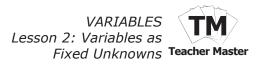
2. Determine the value for the variable that is a fixed unknown.



The variable *h* represents _____

3. Determine the value for the variable that is a fixed unknown.



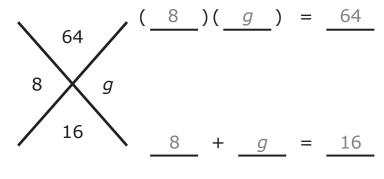


P ractice Key

Pair Practice

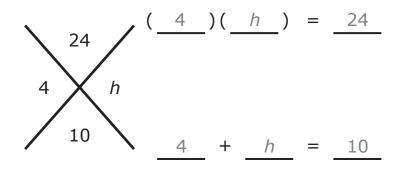
With your partner, for each of the following number puzzles, determine what the fixed unknown variable represents.

1. Determine the value for the variable that is a fixed unknown.



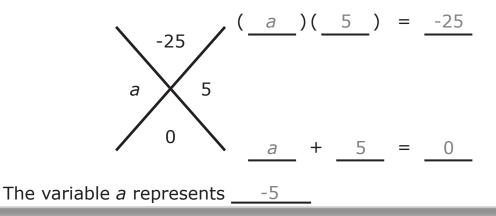
The variable g represents <u>8</u>

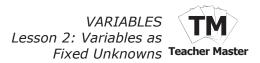
2. Determine the value for the variable that is a fixed unknown.



The variable *h* represents <u>6</u>

3. Determine the value for the variable that is a fixed unknown.





Student 2

E rror Correction Practice

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Question:

For the following equations, determine the value of the fixed unknown variable.

6h =	= 2	24	
6 +	h	=	10

Student 1



E rror Correction Practice Key

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Question:

For the following equations, determine the value of the fixed unknown variable.

$$6h = 24$$

 $6 + h = 10$

Student 1 Student 2 6h=24 6+h=10 6h=24 6+h=10 $\frac{6h}{6}=\frac{24}{6}$ -6 -6 -6 -6 h=4 h=4 h=18 h=4

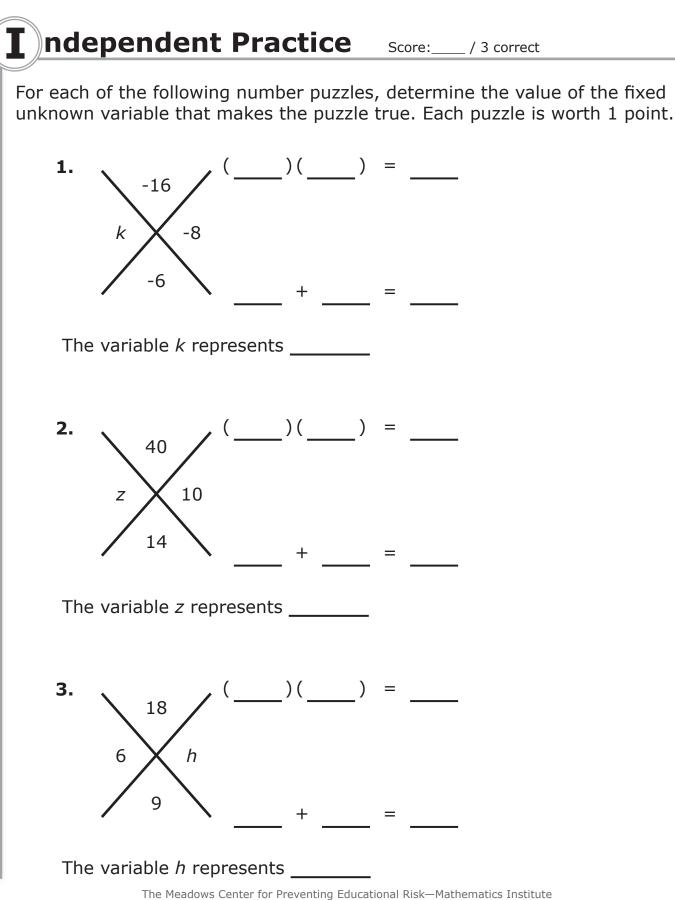
Student 2 is incorrect because when solved, the variable *h* is

representing 2 different values. Student 2 subtracted 6 in the first

equation rather than dividing by 6.

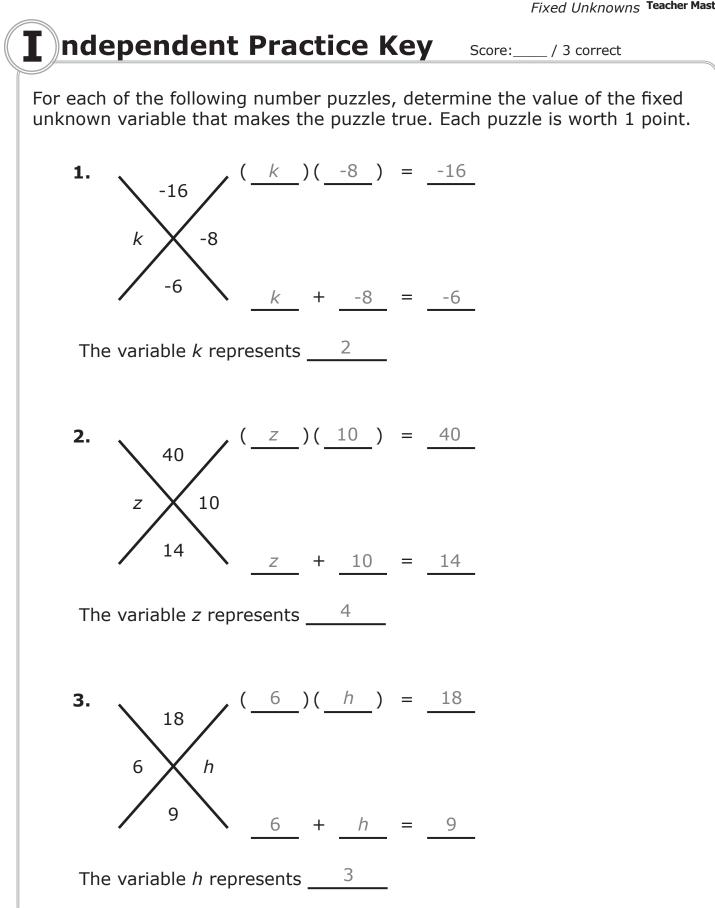
VARIABLES Lesson 2: Variables as Fixed Unknowns Teacher Master

Name:

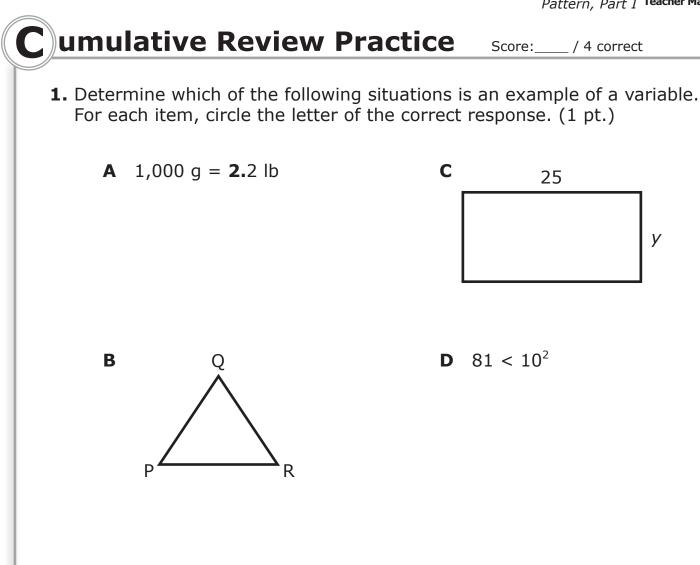


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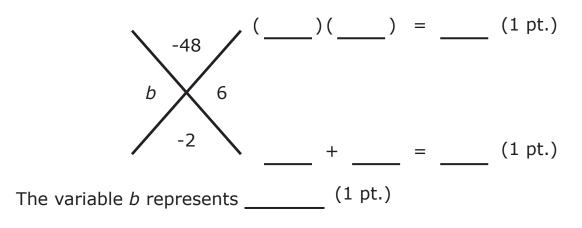
VARIABLES Lesson 2: Variables as Fixed Unknowns Teacher Master



VARIABLES Lesson 3: Variables in a Generalized Pattern, Part I Teacher Master



2. For the following problem, determine the value that makes the number puzzle true.

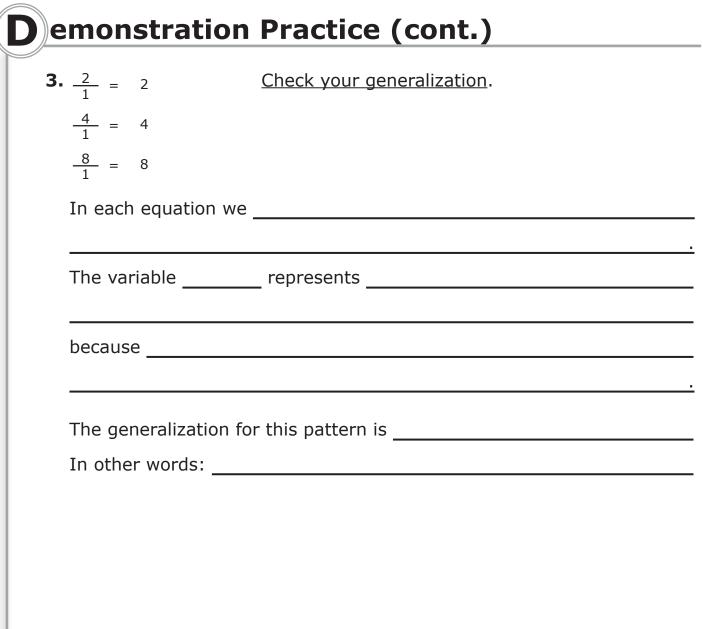


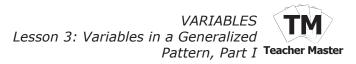
VARIABLES Lesson 3: Variables in a Generalized Pattern, Part I Teacher Master C umulative Review Practice Key Score:____ / 4 correct **1.** Determine which of the following situations is an example of a variable. For each item, circle the letter of the correct response. (1 pt.) **A** 1,000 g = **2.**2 lb С 25 Y **D** $81 < 10^2$ В R 2. For the following problem, determine the value that makes the factor puzzle true. $(_6_)(_b_) = -48$ (1 pt.) -48 6 b -2 b + 6 = -2 (1 pt.) The variable *b* represents _____ (1 pt.)



D emonstration Practice
The following equations represent a pattern. Determine the pattern for each set of equations and use variables to write a generalization of the pattern.
1. $2(1) = 2$ <u>Check your generalization</u> . 3(1) = 3 4(1) = 4 5(1) = 5
In each equation we
The variable represents
because
The generalization for this pattern is In other words:
2. $6 - 6 = 0$ <u>Check your generalization</u> . 7 - 7 = 0 8 - 8 = 0
In each equation we
The variable represents
because
The generalization for this pattern is
In other words:

VARIABLES Lesson 3: Variables in a Generalized Pattern, Part I Teacher Master





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emonstration Practice Key

The following equations represent a pattern. Determine the pattern for each set of equations and use variables to write a generalization of the pattern.

1. $2(1) = 2$ <u>Check your generalization</u> . 3(1) = 3 $a(1) = a$ (answers will vary) 4(1) = 4 $10(1) = 105(1) = 5$					
In each equation we <u>multiply by 1</u>					
The variable <u>a</u> represents <u>the numbers 2, 3, 4 and 5</u>					
because the numbers change from equation to equation					
The generalization for this pattern is $\underline{a(1)} = a$ In other words: <u>a number multiplied by 1 will equal itself</u>					
2. $6 - 6 = 0$ <u>Check your generalization</u> . 7 - 7 = 0 $b - b = 0$ (answers will vary) 8 - 8 = 0 $10 - 10 = 0$					
In each equation we <u>subtract a number from itself and get 0</u>					
The variable <u>b</u> represents <u>the numbers 6, 7, and 8</u>					
because the numbers change from equation to equation					
The generalization for this pattern is $b - b = 0$ In other words: <u>a number subtracted from itself equals 0</u>					

VARIABLES esson 3: Variables in a Generalized



	Practice Key (cont.) Check your generalization. $\frac{c}{1} = c$ (answers will vary) $\frac{10}{1} = 10 $
$\frac{4}{1} = 4$	$\frac{c}{1} = c$ (answers will vary)
In each equation we _	divide a number by 1 and get the same numbe
The variable <u>c</u>	represents the numbers 2, 4, and 8
because the numbe	rs change from equation to equation
The generalization for	this pattern is $\frac{c}{1} = c$
	a number divided by 1 will equal itself

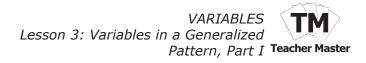


P ractice

Pair Practice

The following equations represent a pattern. With your partner, determine the pattern for each set of equations and match to the correct generalization equation.

Pattern Equations			Generalizations	
	-2(0) = 0		Α	a(1) = a
1.	-1(0) = 0			
	5(0) = 0		В	b(0) = 0
	7 - 7 = 0		C	$\frac{c}{1} = c$
2.	8 - 8 = 0		C	1 0
	15 - 15 = 0			
			D	d-d=0
	-4(1) = -4			
3.	3(1) = 3			
	8(1) = 8			
	$\frac{-2}{1} = -2$			
4.	$\frac{0}{1} = 0$			
	$\frac{2}{1} = 2$			

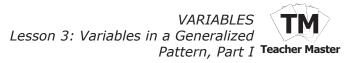


P ractice Key

Pair Practice

The following equations represent a pattern. With your partner, determine the pattern for each set of equations and match to the correct generalization equation.

Pattern Equations			<u>Gene</u>	Generalizations	
	-2(0) = 0		Α	a(1) = a	
1.	-1(0) = 0	В			
	5(0) = 0		В	b(0) = 0	
	7 - 7 = 0		C	$\frac{c}{1} = c$	
2.	8 - 8 = 0	D	C	$\frac{1}{1} = c$	
	15 - 15 = 0				
			D	d-d=0	
	-4(1) = -4				
3.	3(1) = 3	Α			
	8(1) = 8				
	$\frac{-2}{1} = -2$				
4.	$\frac{0}{1} = 0$	С			
	$\frac{2}{1} = 2$				



E rror Correction Practice

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Question:

Write the equation that represents the generalization from the set of numeric equations.

$$-3 + 0 = -3$$

 $-1 + 0 = -1$
 $1 + 0 = 1$
 $3 + 0 = 3$

Student 1

-x + 0 = x

Student 2

x + o = x



E rror Correction Practice Key

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Question:

Write the equation that represents the generalization from the set of numeric equations.

-3 + 0 = -3-1 + 0 = -11 + 0 = 13 + 0 = 3

Student 1

Student 2 x + o = x

-x + 0 = x

Student 1 is incorrect because the variable should not be negated or

taken the opposite of the value.



Name:

ndependent Practice Score: ___ / 4 correct

Determine the pattern for each set of equations and match to the correct generalization equation. Each match is worth 1 point.

P	attern Equations	5	Generalizations
	10 + 0 = 10		A $m(1) = m$
1.	20 + 0 = 20		
	35 + 0 = 35		_
			B $p - p = 0$
	3(1) = 3		
2.	4(1) = 4		C $h + 0 = h$
	11(1) = 11		• • • • • •
	4 - 4 = 0		D $a(0) = 0$
3.	7 - 7 = 0		
	9 - 9 = 0		
	-7(0) = 0		
4.	15(0) = 0		
	-8(0) = 0		

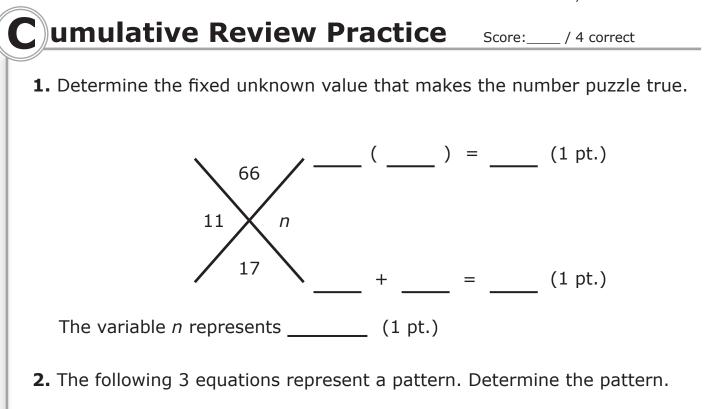
VARIABLES Lesson 3: Variables in a Generalized Pattern, Part I Teacher Master

I ndependent Practice Key Score:____ / 4 correct

Determine the pattern for each set of equations and match to the correct generalization equation. Each match is worth 1 point.

Pa	attern Equations		Gene	ralizations
	10 + 0 = 10		Α	m(1) = m
1.	20 + 0 = 20	С		
	35 + 0 = 35		Р	n = 0
	2(1) - 2		D	p - p = 0
C	3(1) = 3 4(1) = 4	Α		
Ζ.			С	h + 0 = h
	11(1) = 11			
	4 - 4 = 0		D	a(0) = 0
3.	7 - 7 = 0	В		
	9 - 9 = 0			
	7(0) 0			
-	-7(0) = 0	D		
4.	15(0) = 0	D		
	-8(0) = 0			

VARIABLES Lesson 4: Variables as Generalized Patterns, Part II Teacher Master



$$5 - 0 = 5$$

 $7 - 0 = 7$
 $8 - 0 = 8$

Which of the following generalizations best represents the pattern? (1 pt.)

$$h - 0 = h$$

B
$$h + 0 = h$$

C
$$h - h = 0$$

D
$$h(1) = h$$

Easson 4: Variables as Generalized Patterns, Part II Teacher Master **Cumulative Review Practice Key** Score: ____/4 correct 1. Determine the fixed unknown value that makes the number puzzle true. $\frac{66}{11} (\underline{n}) = \underline{66} (1 \text{ pt.})$ The variable *n* represents _____6 (1 \text{ pt.}) The variable *n* represents _____6 (1 \text{ pt.}) 2. The following 3 equations represent a pattern. Determine the pattern.

> 5 - 0 = 57 - 0 = 7 8 - 0 = 8

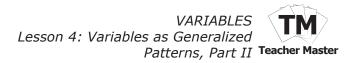
Which of the following generalizations best represents the pattern? (1 pt.)

A
$$h - 0 = h$$

B $h + 0 = h$

C
$$h - h = 0$$

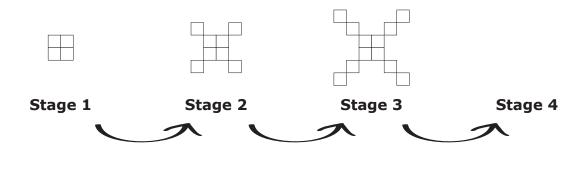
D
$$h(1) = h$$



D emonstration Practice

1.

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

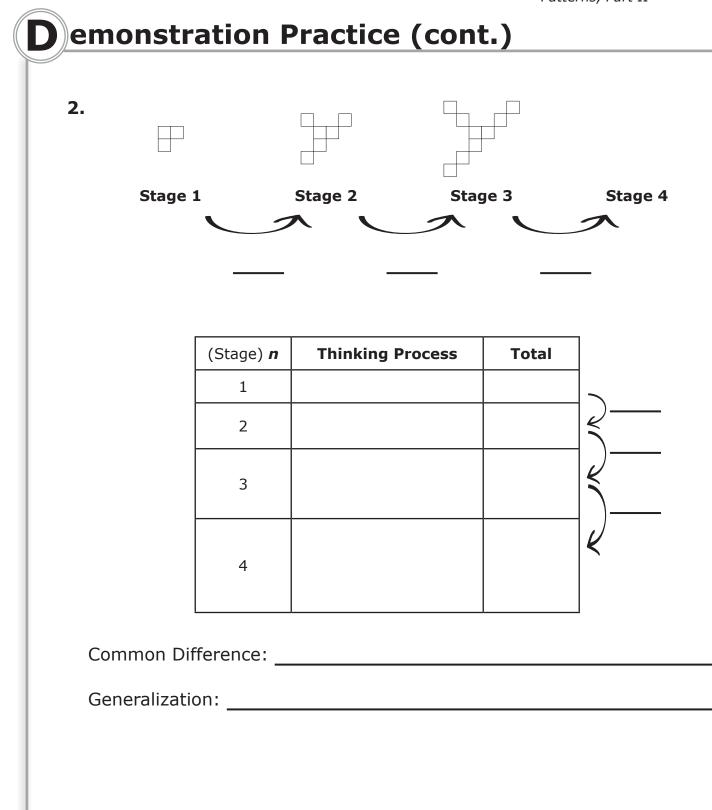


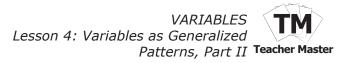
(Stage) n	Thinking Process	Total	
1			
2			₹ <u> </u>
3			K
4			K

Common Difference:

Generalization: _____

VARIABLES Lesson 4: Variables as Generalized Patterns, Part II **Teacher Master**

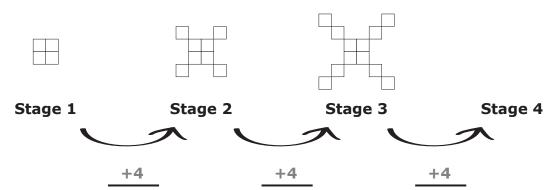




Demonstration Practice Key

1.

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

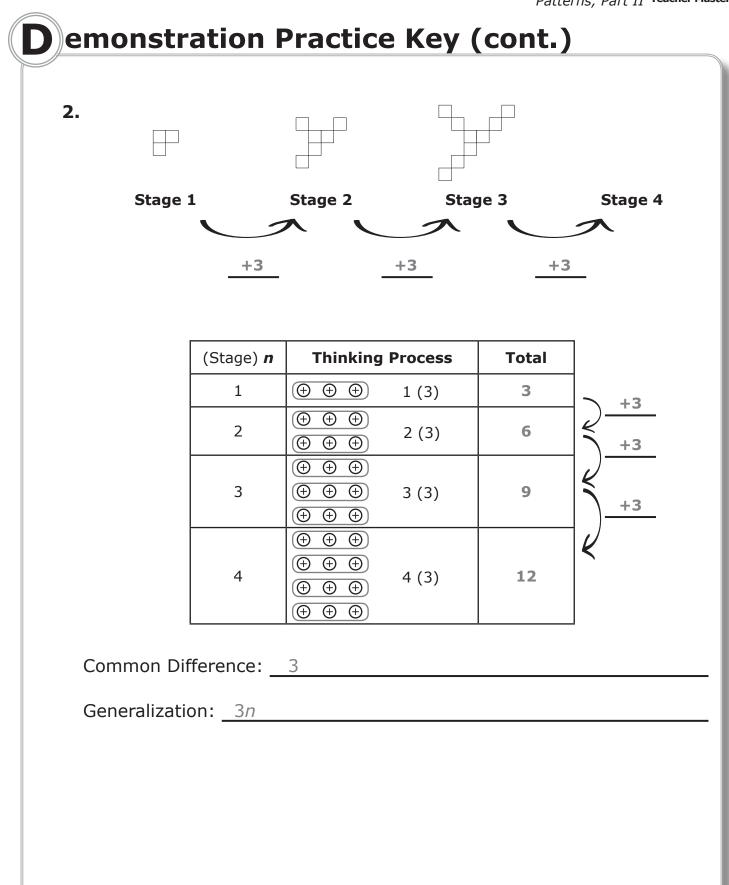


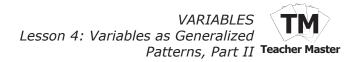
(Stage) n	Thinking Process	Total]
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3	$ \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \hline \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} $	12	K
4	$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} $	16	K

Common Difference: 4

Generalization: 4n

VARIABLES Lesson 4: Variables as Generalized Patterns, Part II Teacher Master

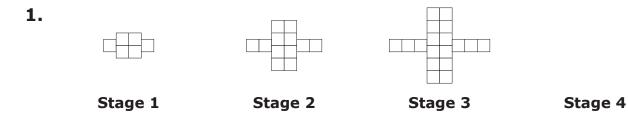




P ractice

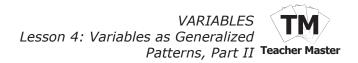
Guided Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.



(Stage) n	Thinking Process	Total	
1			\backslash
2			K
3			$ \xi$
4			

Common Difference:

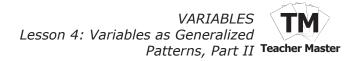


P ractice (cont.)

Pair Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

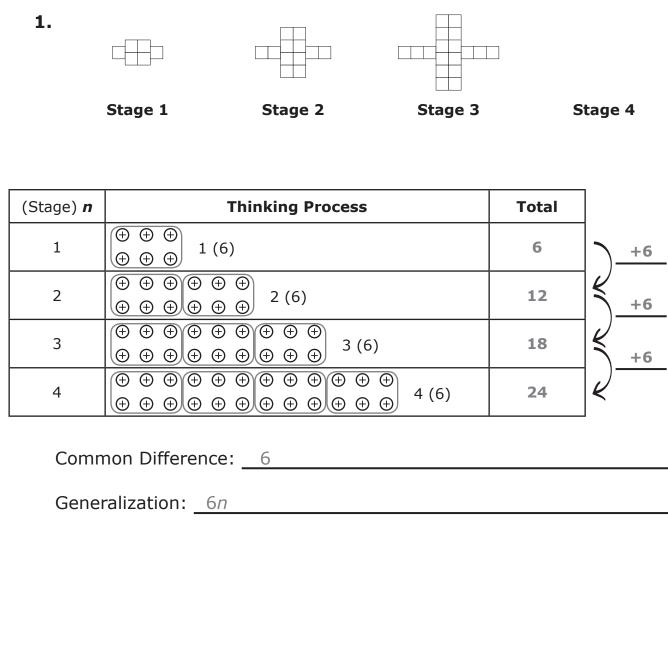
Stage	1	Stage 2	Stage 3	Stage 4
euge	-		y	
	(Stage) n	Thinking Proce	ess Total	
	1			\neg
	2			
	3			
	4			<
Common Di	fference:			
Generalizati	on:			

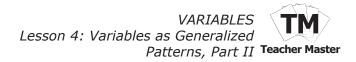


P ractice Key

Guided Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.





Practice Key (cont.)

Stage 1

Pair Practice

Use the pattern in the tile design to fill out each table and use a variable to write a generalization.

Stage 2





Stage 3

Stage 4

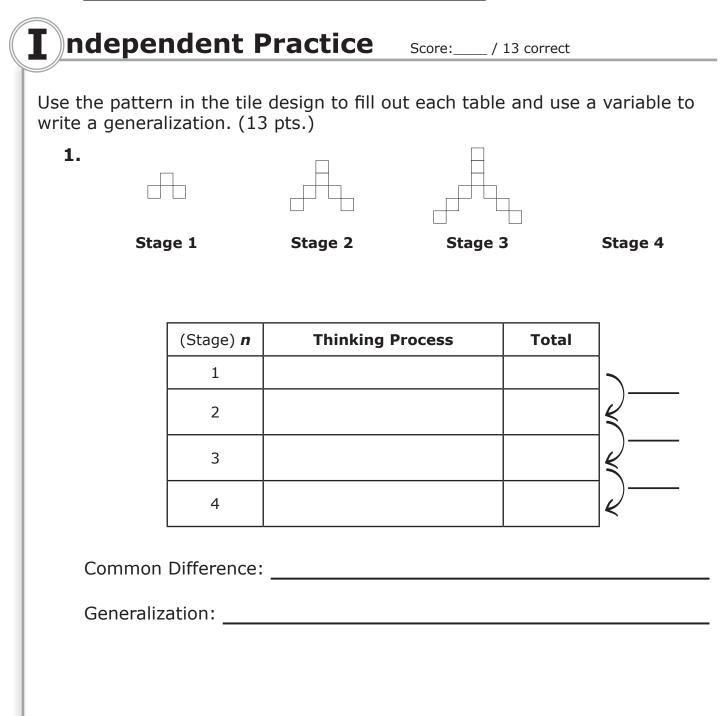
(Stage) n	Thinking	Process	Total]
1	$\textcircled{\begin{array}{c} \hline \\ \hline \\ \end{array}}$	1 (2)	2	 → +2
2	$\begin{array}{c} \textcircled{\bullet} \textcircled{\bullet} \end{array}$	2 (2)	4	<u>الإ</u> +2
3	$\begin{array}{c} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \end{array}$) 3 (2)	6	₹ +2
4	$(\begin{array}{c} \begin{array}{c} \hline \\ \hline $) 4 (2)	8	√

Common Difference: 2

Generalization: 2n

VARIABLES Lesson 4: Variables as Generalized Patterns, Part II Teacher Master

Name: _____



Scoring Key:

1 point for each table,



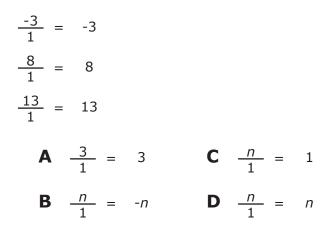
Patterns, Part II Teacher Master 1 point for generalization **I ndependent Practice Key** Score:____ / 13 correct Use the pattern in the tile design to fill out each table and use a variable to write a generalization. (13 pts.) 1. Stage 2 Stage 3 Stage 4 Stage 1 (Stage) **n Thinking Process** Total 1 $(\oplus \oplus \oplus)$ 3 1(3) +3 $(\oplus \oplus \oplus)$ 2 6 2 (3) $(\oplus \oplus \oplus)$ +3 $(\overline{\oplus} \ \overline{\oplus} \$ 3 9 3 (3) $(\oplus \oplus \oplus)$ +3 $(\overline{\oplus} \ \overline{\oplus} \$ 4 4 (3) 12 $(\overline{\oplus} \ \overline{\oplus} \$ Common Difference: 3 Generalization: 3n

VARIABLES Lesson 5: Variables as Generalized Patterns, Part III Teacher Master



umulative Review Practice Score:____ / 2 correct

1. Determine the pattern and select the correct generalization. (1 pt.)



 Use the pattern in the tile design to fill out the table and use a variable to write a generalization of this pattern.

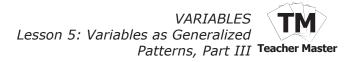
Stage :	L	Stage 2	Stage 3	Stage 4
	Stage	Process	Total]
	1	(†) (†)	2	
	2	$\oplus \oplus \oplus \oplus$	4]≼
	3	$\begin{array}{c} \oplus \ \oplus \ \oplus \ \oplus \end{array} \\ \oplus \ \oplus \end{array}$	6]<
	4	$\begin{array}{cccc} \oplus & \oplus & \oplus & \oplus \\ \oplus & \oplus & \oplus & \oplus \end{array}$	8]<

Which of the following is the correct generalization for the pattern in the table? (1 pt.) $\$

A 2*n* **C** 6*n*

B n + 3

D *n* + 2



C umulative Review Practice Key Score: / 2 correct

1. Determine the pattern and select the correct generalization. (1 pt.)

$$\frac{-3}{1} = -3$$

$$\frac{8}{1} = 8$$

$$\frac{13}{1} = 13$$

$$A \quad \frac{3}{1} = 3$$

$$C \quad \frac{n}{1} = 1$$

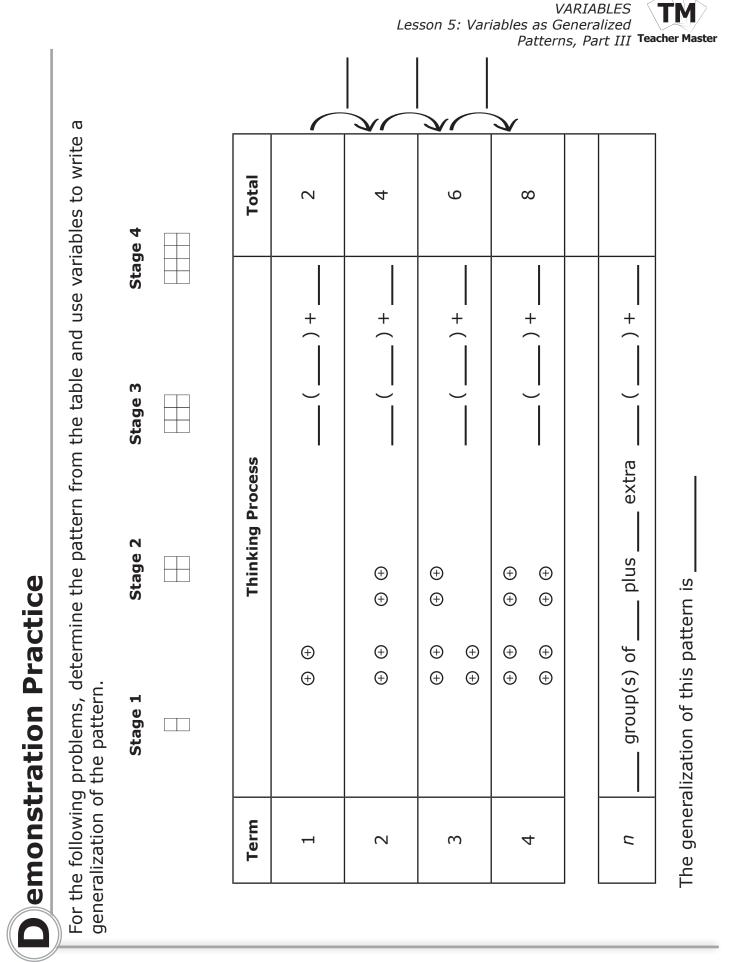
$$B \quad \frac{n}{1} = -n$$

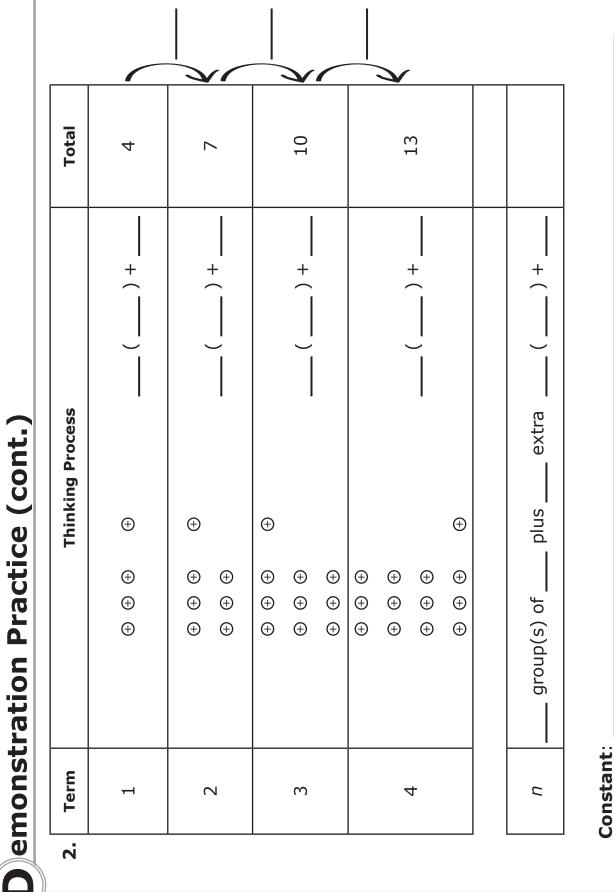
$$D \quad \frac{n}{1} = n$$

2. Use the pattern in the tile design to fill out the table and use a variable to write a generalization of this pattern.

Stage 1	L	Stage 2	Stage	3	Stage 4
[Stage	Process		Total	
	1	()		2	→ + 2
	2	$(\overline{+}, \overline{+}) (\overline{+}, \overline{+})$		4	4 + 2
	3	$ \begin{array}{c} $		6	+2
	4	$ \begin{array}{c} \left(\end{array}{c} \left(\begin{array}{c} \left(\begin{array}{c} \left(\begin{array}{c} \left(\end{array}{c} \left(\end{array}{c} \left(\end{array}{c} \left(\end{array}{c} \left(\begin{array}{c} \left(\end{array}{c} \left(\end{array}{c$		8	\mathcal{L}
Which of the table? (1 pt		is the correct g	enerali	zation for t	he pattern in the

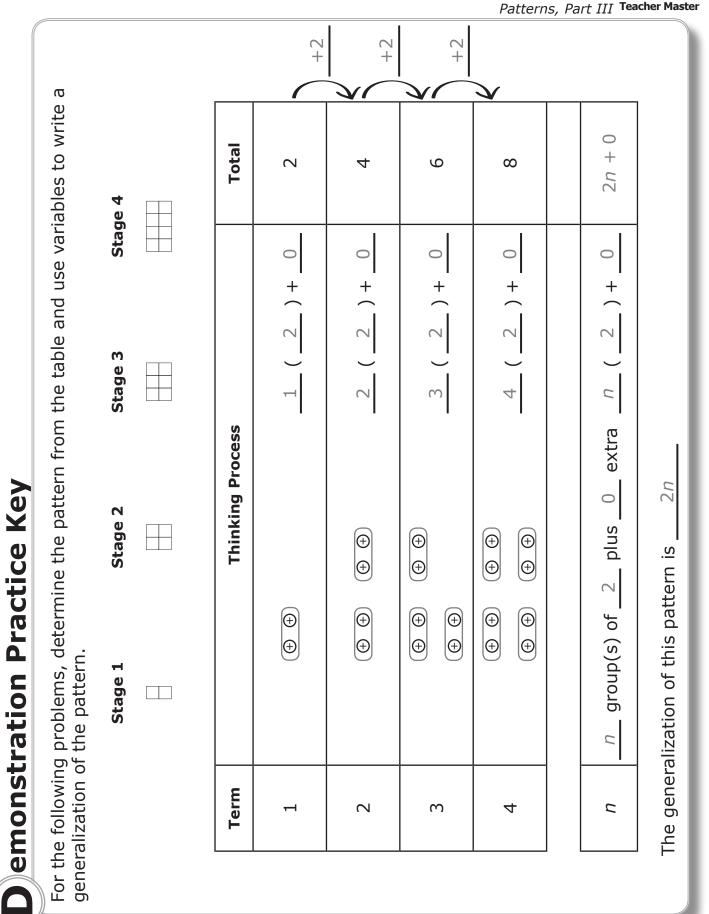






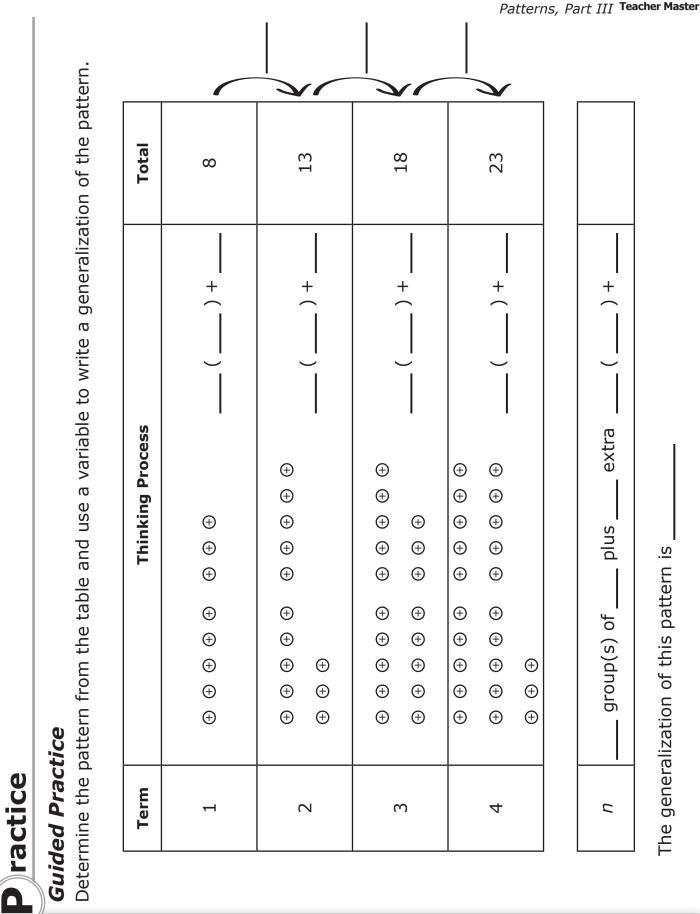
The generalization of this pattern is

VARIABLES Lesson 5: Variables as Generalized

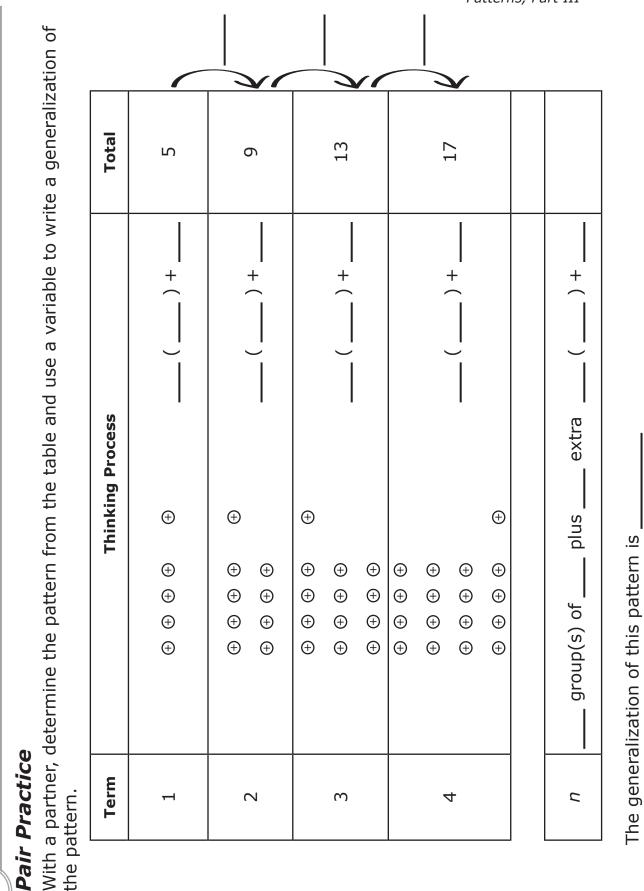


∾ + ∩ + ∞ + -Total 13 +10 4 ЗЛ Constant: a term that contains no variables and does not change value -+ + + +Demonstration Practice Key (cont.) 4 **Thinking Process** extra +-ЗЛ plus \oplus \oplus \oplus \oplus The generalization of this pattern is € Ð Ð Ð Ð \sim \oplus \oplus \oplus \oplus \oplus Ð Ð Ð Ð Ð \oplus \oplus \oplus \oplus \oplus group(s) of Ð Ð Ð Ð Ð Ð \oplus (\oplus) \oplus \oplus U Term \sim \mathbf{c} 4 Ч.





VARIABLES Lesson 5: Variables as Generalized





P ractice (cont.)

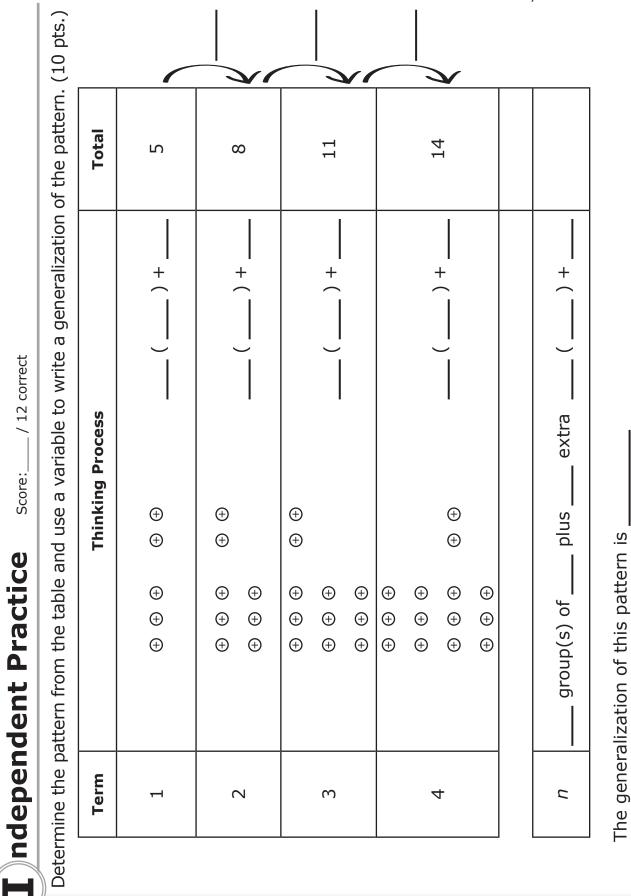
Patterns, Part III Teacher Master ம + ſ ſ ++Determine the pattern from the table and use a variable to write a generalization of the pattern. \odot Total 13 $\frac{1}{8}$ 23 +00 57 \odot \sim \odot \odot \odot + + ഹ ഥ Ь \square \bigcirc 4 **Thinking Process** extra \oplus \oplus \oplus \oplus \bigcirc + \oplus \oplus \oplus \oplus \odot 57 \oplus \oplus \oplus \oplus \oplus \oplus plus \oplus \oplus \oplus \oplus \oplus \oplus The generalization of this pattern is \oplus \oplus \oplus \oplus \oplus \oplus ഥ \oplus \oplus \oplus (\oplus) \oplus (\oplus) group(s) of \oplus (\oplus) Ð \oplus \oplus \oplus Ð **Guided Practice** \Box Term \mathbf{c} \sim 4

P ractice Key

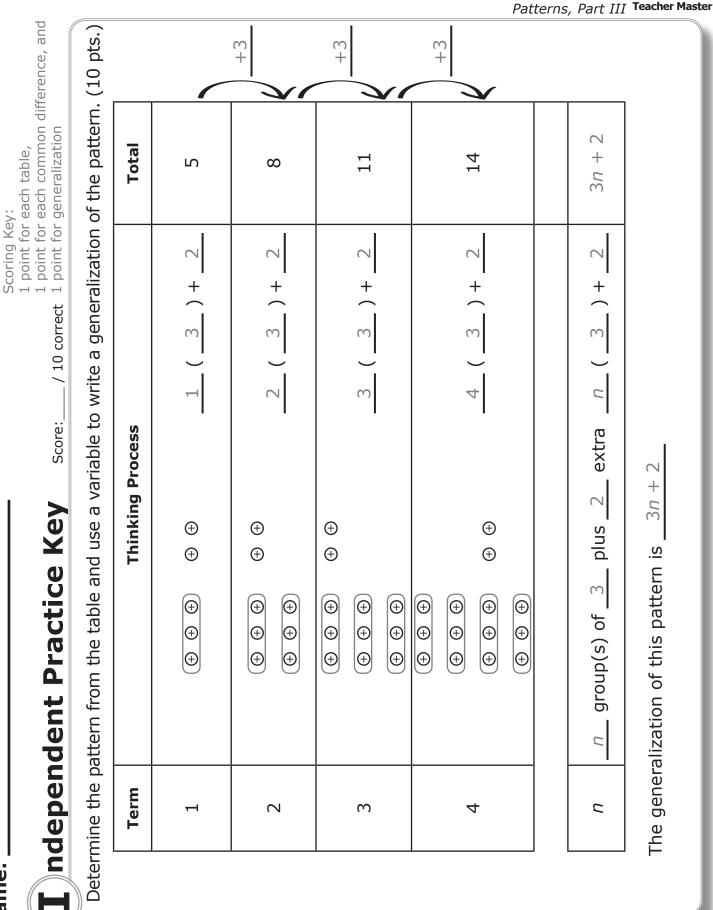
VARIABLES Lesson 5: Variables as Generalized



With a partner, determine the pattern from the table and use a variable to write a generalization of +4 +4 +-Total 13 17+ഹ σ 4n+ + 4 4 4 4 4 4 extra **Thinking Process** +-41 \oplus \oplus \oplus \oplus plus The generalization of this pattern is \oplus \oplus \oplus \oplus \oplus Ð \oplus \oplus \oplus \oplus 4 \oplus P ractice Key (cont.) \oplus Ð \oplus \oplus \oplus \oplus \oplus \oplus \oplus group(s) of \oplus \oplus Ð \oplus \oplus \oplus \oplus Ω **Pair Practice** Term the pattern. \sim \mathbf{m} 4







VARIABLES

Lesson 5: Variables as Generalized

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Name:

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VARIABLES Lesson 6: Variables in a Generalized Pattern, Part IV Teacher Master



C umulative Review Practice Score:____ / 2 correct

1. Use the pattern blocks and the table below to answer the questions.





Stage 3

Stage	Thinking Process	Total Number of Tiles	
1		4	
2		8	≼
3		12	√

Which of the following is the correct generalization? (1 pt.)

- **A** 2*n*
- **B** *n* + 8
- **C** 4n
- **D** *n* + 4
- **2.** Look at the table below.

Term	Thinking	Process	Total
1	$\oplus \oplus \oplus \oplus \oplus \oplus$	(1)(3) + 2	5
2	$\begin{array}{c} \oplus \ \end{array}$	(2)(3) + 2	8
3	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	(3)(3) + 2	11
4	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	(4)(3) + 2	14
n			??

Which of the following is the correct generalization for the pattern in the table? (1 pt.)

- **A** 3*n*
- **B** *n* + 5
- **C** *n* + 2
- **D** 3*n* + 2

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VARIABLES Lesson 6: Variables in a Generalized Pattern, Part IV Teacher Master



C umulative Review Practice Key Score: / 2 correct

1. Use the pattern blocks and the table below to answer the questions.



Stage 1

Stage 3

Stage	Thinking Process	Total Number of Tiles]
1		4	$] \rightarrow +4$
2		8	$] \leq + 4$
3		12]<

Which of the following is the correct generalization? (1 pt.)

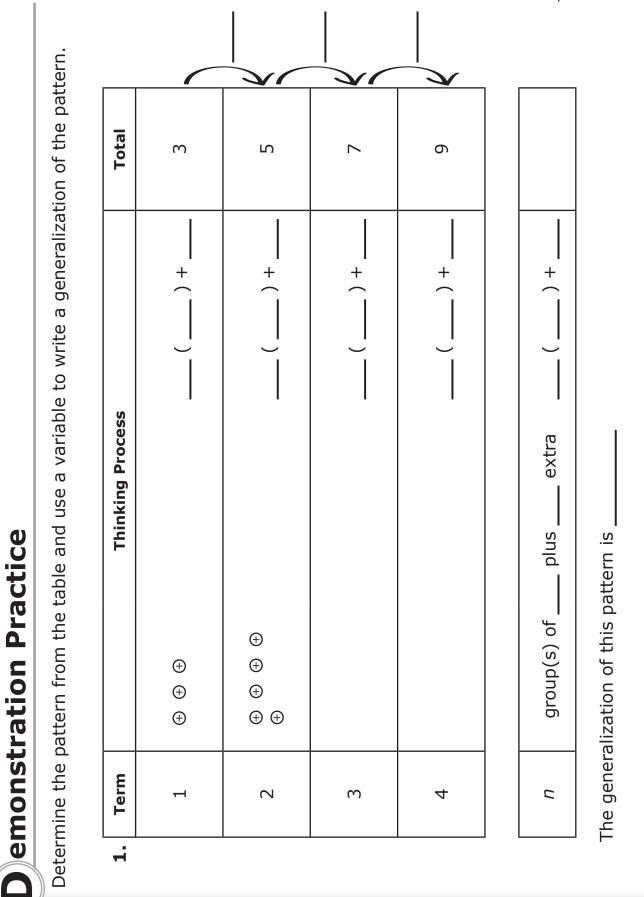
A 2n **B** n + 8 **C** 4n**D** n + 4

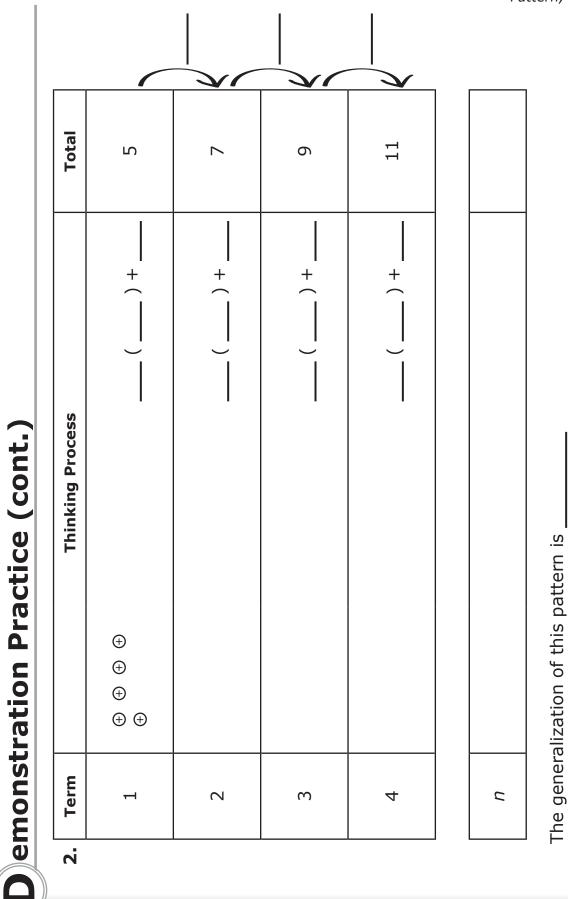
2. Look at the table below.

Term	Thinking Process	Total
1	$\oplus \oplus \oplus \oplus \oplus \oplus $ (1)(3) + 2	5
2	$ \begin{array}{c} \oplus \ \oplus \ \oplus \ \oplus \ \oplus \ \oplus \\ \oplus \ \oplus \ \oplus \ \end{array} (2)(3) + 2 $	8
3	$ \begin{array}{cccc} \oplus \oplus \oplus \oplus \oplus \oplus \\ \oplus \oplus \oplus \oplus \oplus \oplus \end{array} \\ \oplus \end{array} (3)(3) + 2 $	11
4	$ \begin{array}{cccc} \oplus \oplus \oplus \oplus \oplus \oplus \\ \oplus \oplus \oplus \oplus \oplus \oplus & \oplus \\ \oplus \oplus \oplus & \oplus &$	14
n		??

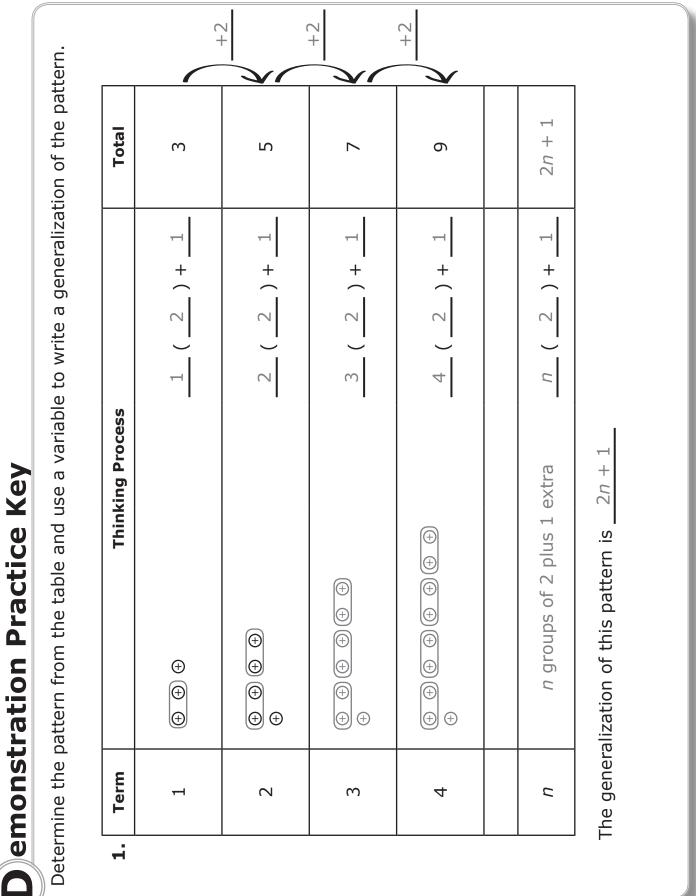
Which of the following is the correct generalization for the pattern in the table? (1 pt.)

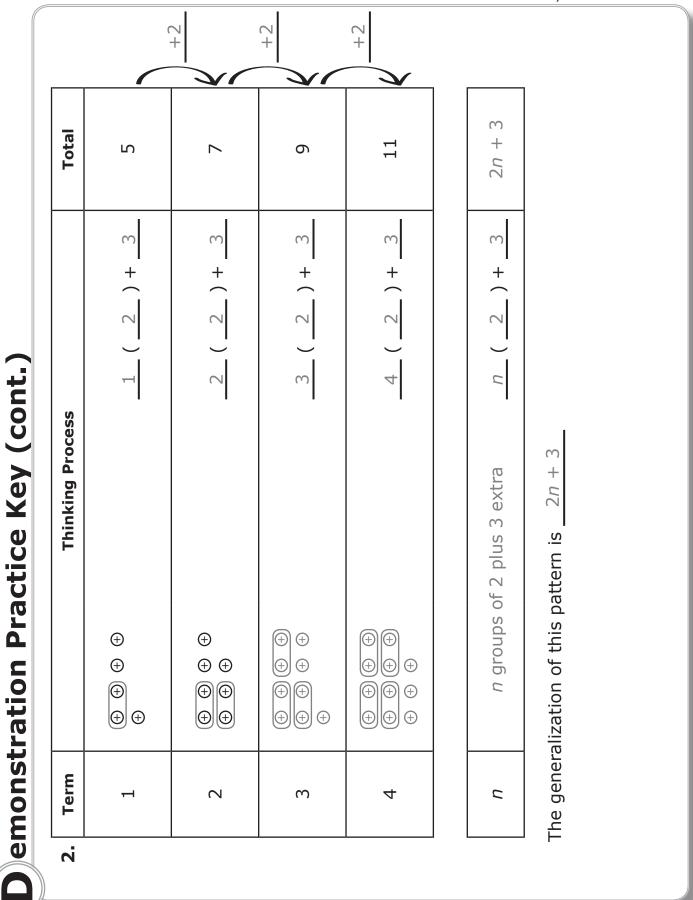
- **A** 3n
- **B** *n* + 5
- **C** *n* + 2
- **D** 3*n* + 2





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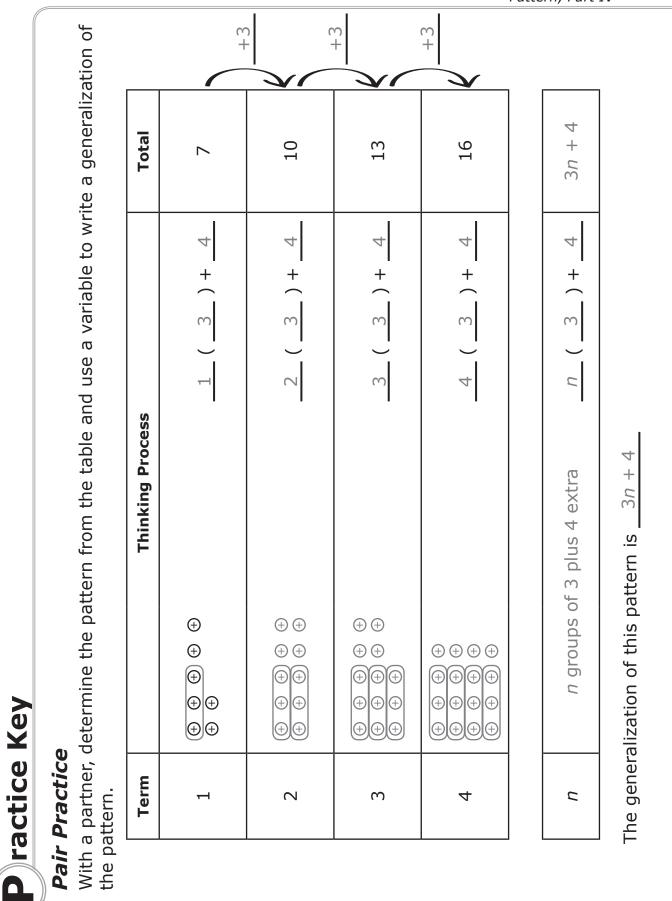
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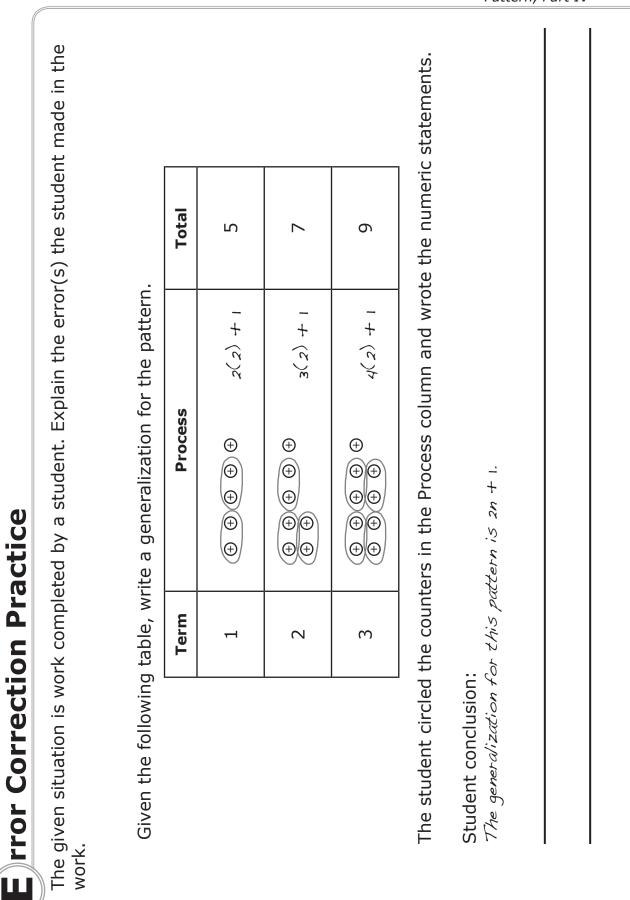


Pair Practice

With a partner, determine the pattern from the table and use a variable to write a generalization of the pattern

VARIABLES Lesson 6: Variables in a Generalized Pattern, Part IV Teacher Master







The given situation is work completed by a student work. Given the following table, write a generalizati 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	I table, wr Term 1 2 2	iven situation is work completed by a student. Explain the error(s) the student made in the Given the following table, write a generalization for the pattern. $ \begin{array}{c c} \hline Term & Process & Total \\ \hline 1 & \oplus \oplus \oplus \oplus & 2(2) + i & 5 \\ \hline 2 & \oplus \oplus \oplus & 3(2) + i & 7 \\ \hline 2 & \oplus \oplus & 3(2) + i & 7 \\ \hline \end{array} $	olain the error or the pattern z(z) + 1 z(z) + 1	(s) the studer Total	t made in the
	ω	+ + <t< td=""><td>4(2) + 1</td><td>6</td><td></td></t<>	4(2) + 1	6	
The student circled the coun	the count	Iters in the Process column and wrote the numeric statements.	umn and wro	te the numeri	c statements.
Student conclusion: The generalization for this pattern is 2n + 1.	or this pa	ttern is 2n + I.			
The student circled 2 sets of 2	2 sets of	2 counters for the 1st term. The student should have only	it term. The s	tudent should	have only
circled 1 set of counters to		making the numeric statement $1(2) + 3$. Each term has 1	tatement 1(2)) + 3. Each te	rm has 1 set
too many circled.	The correc	too many circled. The correct generalization is $2n +$	ო +		





/ 10 correct Score: **Independent Practice** -

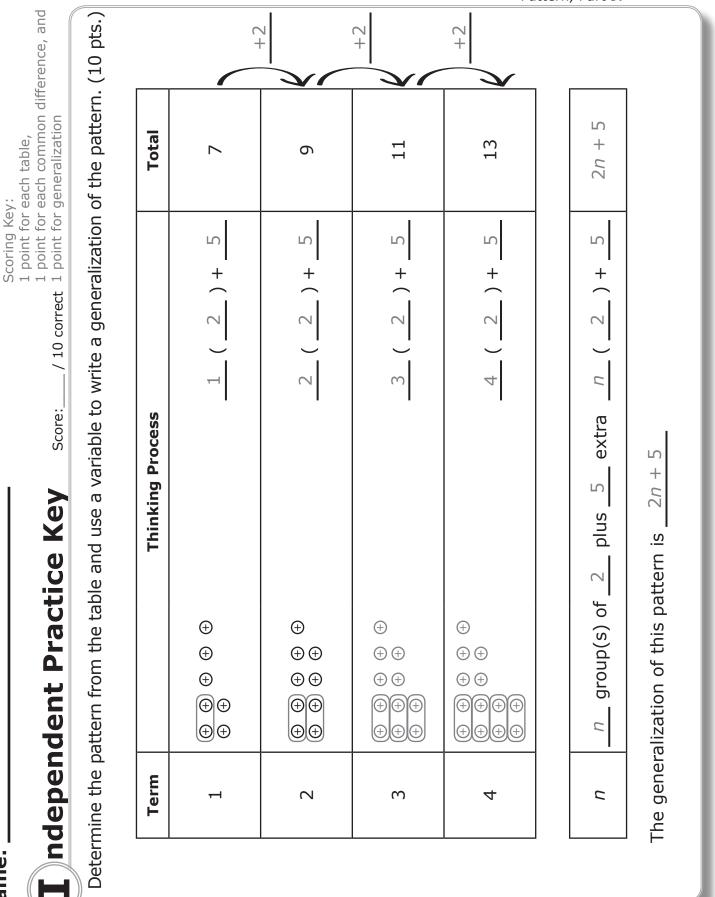
Determine the pattern from the table and use a variable to write a generalization of the pattern. (10 pts.)

r					
Total	7	6	11	13	
Thinking Process	 + () → + () → 		+ ()) + ()	group(s) of plus extra () +
Term	1	2	e	4	c

VARIABLES Lesson 6: Variables in a Generalized Pattern, Part IV Teacher Master



The generalization of this pattern is



VARIABLES Lesson 6: Variables in a Generalized Pattern, Part IV Teacher Master

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Name:



umulative Review Practice Score:____ / 2 correct

(Stage) n	Thinking Process	Total	
1	⊕ ⊕ ⊕ 1(3)	3	\ +3
2	 ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ 2(3) 	6	\leq
3	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	9	+3
4	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12	K
n		??	

1. Use the completed table to answer the following question.

Which of the following is the correct generalization of the table's pattern? (1 pt.)

A 3*n*

B 3*n* + 3 **C** *n* + 3 **D** n + 2

2. Use the completed table to answer the following question.

(Stage) n	Thinking Process	Total	
1	(+ + + + + + + + + + + + + + + + + + +	5	- +3
2	$ \begin{array}{c} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \textcircled{} \begin{array}{c} \textcircled{} \textcircled{} \end{array} \end{array} \\ \begin{array}{c} \textcircled{} \textcircled{} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \textcircled{} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} $	8	<u>≺</u> +3
3	 ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ ⊕ 3(3)+2 	11	+3
4	$ \begin{array}{c} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \\ \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \\ \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \\ \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \textcircled{\bullet} \end{array} $	14	K
n		??	

Which of the following is the correct generalization of the table's pattern? (1 pt.)

A n + 1B 3n + 2С 3n D 5n + 2

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C umulative Review Practice Key Score: / 2 correct

(Stage) n	Thinking Process	Total	
1	(+ + + + 1(3)	3	
2	(+ + +) (+ + +) + (3)	6	$ \xi$
3	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	9	+3
4	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12	K
n		??	

1. Use the completed table to answer the following question.

Which of the following is the correct generalization of the table's pattern? (1 pt.)

3*n*

- **B** 3*n* + 3 **C** *n* + 3

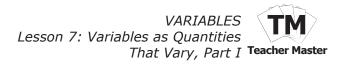
D *n* + 2

2. Use the completed table to answer the following question.

(Stage) n	Thinking Process	Total	
1	(⊕ ⊕ ⊕ ⊕ ⊕ 1(3)+2	5	-+3
2	$\begin{array}{c} \textcircled{} \end{array}{\end{array}}$	8	
3	$ \begin{array}{c} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \textcircled{} \textcircled{} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \textcircled{} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \textcircled{} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \textcircled{} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} $	11	$\left \underbrace{\boldsymbol{\xi}}_{+3} \right $
4	$ \begin{array}{c} \textcircled{} \end{array}{} \end{array} $	14	\ <
n		??	

Which of the following is the correct generalization of the table's pattern? (1 pt.)

A n + 1 **B** 3n + 2 **C** 3n **D** 5n + 2



emonstration Practice

Brainstorm:

Addition	Subtraction	Multiplication	Division	Equals

For the following situations, define the variables that are appropriate and write an equation to describe the relationship.

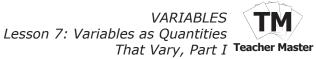
1. The sum of a number and 7 is 15.

Equation:

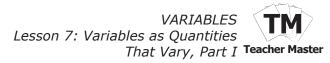
2. The product of the first number and 3 is equal to the second number.

Variable(s):_____

Equation: _____



	That Vary, Part I Teac
en	nonstration Practice (cont.)
3. TI	ne quotient of the first number and 2 is equal to the second number
	Variable(s):
	Equation:
4. TI	ne second number is 3 less than the first number.
	Variable(s):
	Equation:



D emonstration Practice Key

Brainstorm:

Addition	Subtraction	Multiplication	Division	Equals
add plus	subtract minus	multiply product	divide quotient	is is equal to
sum	difference	times	halved	makes
more than	less than	double twice	third quartered	totals gives
		triple	-	

For the following situations, define the variables that are appropriate and write an equation to describe the relationship.

1. The sum of a number and 7 is 15.

Variable(s): <u>n = the value of the number</u>

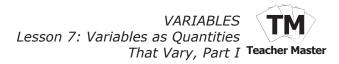
Equation: n + 7 = 15

2. The product of the first number and 3 is equal to the second number.

Variable(s): *f* = the value of the first number

h = the value of the second number

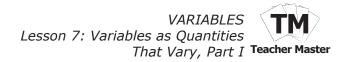
Equation: 3f = h



Demonstration Practice Key (cont.)

3. The quotient of the first number and 2 is equal to the second number.

	Variable(s):	s): $a =$ the value of the first number			
	b = the value of the second number				
	Equation:	$\frac{a}{2} = b$			
	(note: the	e letter choice of the variable may vary)			
4. Ti	he second numb	er is 3 less than the first number.			
	Variable(s):	c = the value of the first number			
		d = the value of the second number			
	Equation:	d = c - 3			



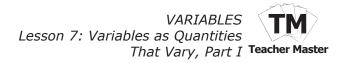
Pair Practice

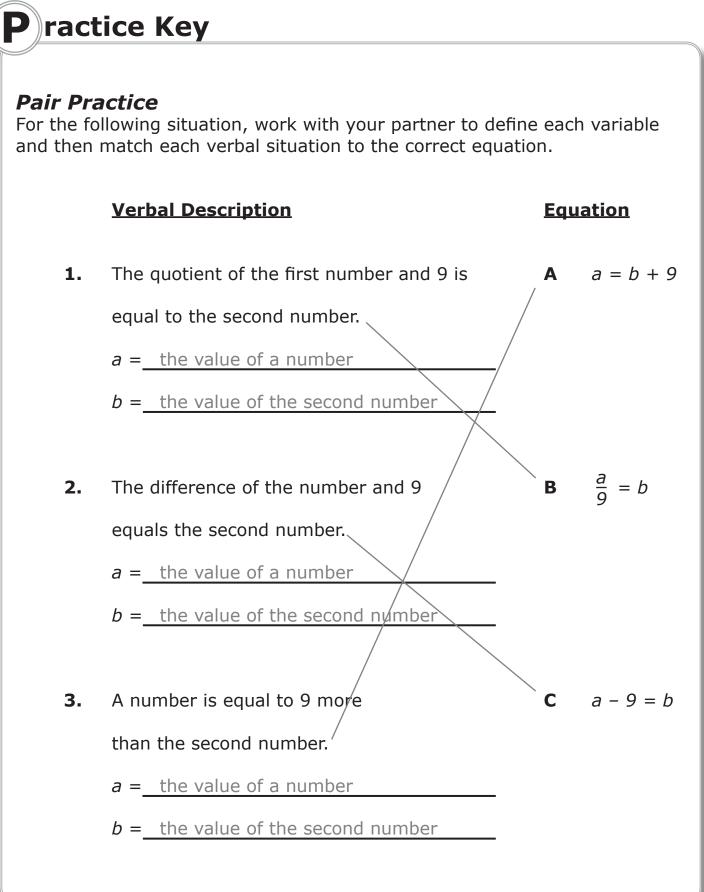
ractice

P

For the following situation, work with your partner to define each variable and then match each verbal situation to the correct equation.

Verbal Description	Equ	uation
equal to the second number.	Α	a = b + 9
a = b =		
The difference of the number and 9 equals the second number. a =	B	$\frac{a}{9} = b$
A number is equal to 9 more than the second number. a =	C	a – 9 = b
	The quotient of the first number and 9 is equal to the second number. $a = \b = \b$ The difference of the number and 9 equals the second number. $a = \b$ $b = \b$ A number is equal to 9 more than the second number.	The quotient of the first number and 9 is equal to the second number.A $a = \b = \Bb = \BThe difference of the number and 9equals the second number.Ba = \b = \b = \CA number is equal to 9 morethan the second number.Ca = \C$





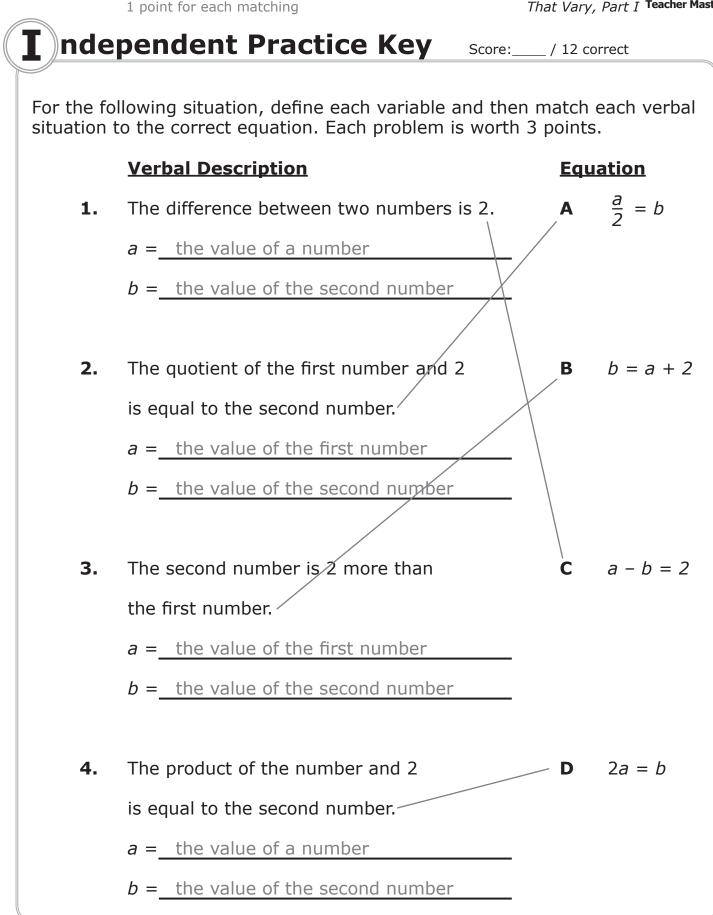
VARIABLES Lesson 7: Variables as Quantities That Vary, Part I Teacher Master

Name:

nde	pendent Practice Score:/ 12	correct	
	llowing situation, define each variable and the to the correct equation. Each problem is wort		
	Verbal Description	<u>Equ</u>	ation
1.	The difference between two numbers is 2.	Α	$\frac{a}{2} = b$
	a =		
	<i>b</i> =		
2.	The quotient of the first number and 2	В	b = a + 2
	is equal to the second number.		
	a =		
	<i>b</i> =		
3.	The second number is 2 more than	С	a – b = 2
	the first number.		
	a =		
	<i>b</i> =		
4.	The product of the number and 2	D	2a = b
	is equal to the second number.		
	a =		
	b =		

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C umulative Review Practice Score: / 2 correct

> Term **Thinking Process** Total $(\overline{\oplus} \ \overline{\oplus} \$ 5 1 1(4)+1+4 2 9 $(\oplus \oplus \oplus \oplus)$ 2(4)+1+4 $(\overline{\oplus} \oplus \overline{\oplus} \oplus \overline{\oplus}) \oplus$ 3 $(\oplus \oplus \oplus \oplus)$ 13 $(\oplus \oplus \oplus \oplus)$ 3(4)+1+4 $\oplus \oplus \oplus \oplus$ 17 4 $\oplus \oplus \oplus \oplus$ $(\oplus \oplus \oplus \oplus)$ 4(4)+1?? n

1. Use the completed table to answer the following question.

Which of the following is the correct generalization of the table's pattern? (1 pt.)

 \mathbf{A} n+4**C** 4*n*

- **B** 4n + 1 **D** 5n + 1
- 2. Read the following situations and select the equation that represents the relationship given in the word problem. (1 pt.)

The product of the first number and 12 is equal to the second number. a = the value of the first number. b = the value of the second number.

A 12b = a**C** 12a = b

B $a \cdot b = 12$ **D** 12 - a = b





C umulative Review Practice Key Score:____ / 2 correct

Term	Thinking Process	Total	
1	$\begin{array}{cccc} \textcircled{\oplus} \begin{array}{c} \textcircled{\oplus} \begin{array}{c} \textcircled{\oplus} \end{array} \begin{array}{c} \end{array} \begin{array}{c} \end{array} \begin{array}{c} \end{array} \begin{array}{c} \end{array} \end{array}$	5	→ +4
2	$\begin{array}{cccc} \hline \oplus & \oplus & \oplus & \oplus \\ \hline \oplus & \oplus & \oplus & \oplus \\ \hline \hline \oplus & \oplus & \oplus & \oplus \\ \end{array} \begin{array}{c} 2(4)+1 \end{array}$	9	\leq
3	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13	+4
4	$\begin{array}{c} \textcircled{\begin{array}{c} \hline \oplus \ \oplus$	17	K
n		??	

1. Use the completed table to answer the following question.

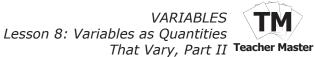
Which of the following is the correct generalization of the table's pattern? (1 pt.)

C 4*n* **A** n+4 **D** 5n + 1**B** 4*n* + 1

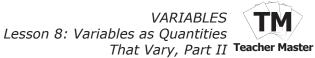
2. Read the following situations and select the equation that represents the relationship given in the word problem. (1 pt.)

The product of the first number and 12 is equal to the second number. a = the value of the first number. b = the value of the second number.

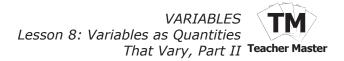
- **C** 12a = b**A** 12b = a
- **B** $a \cdot b = 12$ **D** 12 - a = b



	That vary, Part II Teacher Pha
	D emonstration Practice
//	For the following situation, define the variables that are appropriate and write an equation to describe the relationship.
	1. The second number is 5 more than twice the first number.
	Variable(s):
	Equation:
	2. Double the first number is equal to the difference of the second number and 1.
	Variable(s):
	Equation:
	3. The quotient of the first number and 3 plus 7 is the second number.
	Variable(s):
	Equation:
	 The product of the first number and 8 is equal to the sum of the second number and 4.
	Variable(s):
	Equation:



	That Vary, Part II Teacher Mast			
C	Demonstration Practice Key			
	For the following situation, define the variables that are appropriate and write an equation to describe the relationship.			
	1. The second number is 5 more than twice the first number.			
	Variable(s): $x =$ the value of the first number			
	w = the value of the second number			
	Equation: $w = 2x + 5 \text{ or } w = 5 + 2x$			
	2. Double the first number is equal to the difference of the second number and 1.			
	Variable(s): <i>f</i> = the value of the first number			
	b = the value of the second number			
	Equation: $2f = b - 1$			
	3. The quotient of the first number and 3 plus 7 is the second number.			
	Variable(s):h = the value of the first number			
	c = the value of the second number			
	Equation: $\frac{h}{3} + 7 = c$			
	 The product of the first number and 8 is equal to the sum of the second number and 4. 			
	Variable(s): $g =$ the value of the first number			
	d = the value of the second number			
	Equation: $8g = d + 4$			

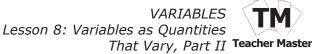


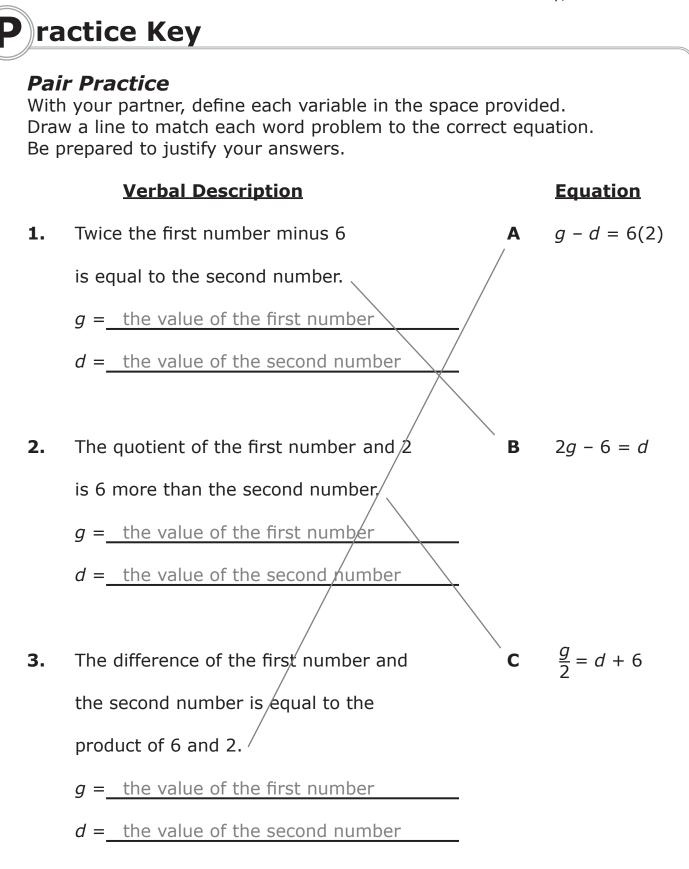
P ractice

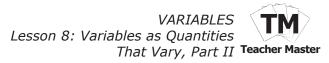
Pair Practice

With your partner, define each variable in the space provided. Draw a line to match each word problem to the correct equation. Be prepared to justify your answers.

	Verbal Description		Equation
1.	Twice the first number minus 6	Α	g-d=6(2)
	is equal to the second number.		
	<i>g</i> =		
	d =		
2.	The quotient of the first number and 2	В	2g - 6 = d
	is 6 more than the second number.		
	<i>g</i> =		
	d =		
3.	The difference of the first number and	С	$\frac{g}{2} = d + 6$
	the second number is equal to the		
	product of 6 and 2.		
	<i>g</i> =		
	d =		







E rror Correction Practice

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Write the equation from the given verbal description.

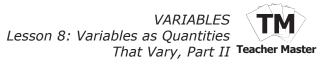
The product of the first number and 5 is equal to 3 less than the second number.

Student 1:

Student 2:

5 + x = 3 - y

5x = y - 3



E rror Correction Practice Key

The given situations are work completed by two different students. Determine which student is incorrect and explain the error.

Write the equation from the given verbal description.

The product of the first number and 5 is equal to 3 less than the second number.

Student 1:

Student 2:

5x = y - 3

5 + x = 3 - y

Student 2 is incorrect. The product of the first number

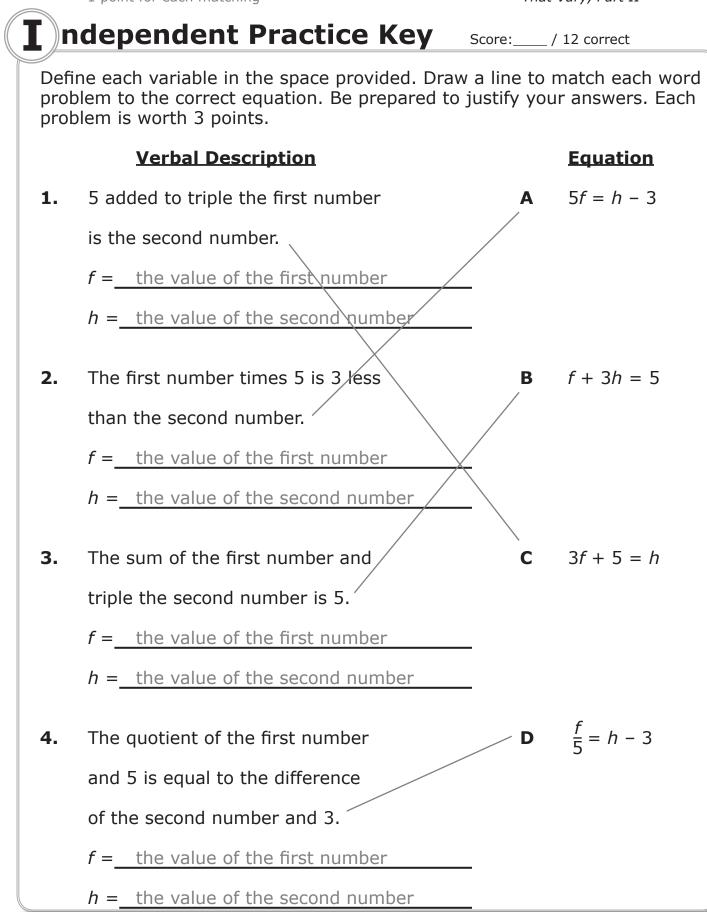
and 5 should be 5x, not 5 + x.

Name: _____

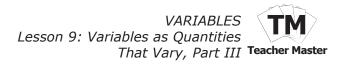
Tr	ndependent Practice Score:	_ / 12 corre	ct			
pro	Define each variable in the space provided. Draw a line to match each word problem to the correct equation. Be prepared to justify your answers. Each problem is worth 3 points.					
	Verbal Description		Equation			
1.	5 added to triple the first number	Α	5f = h - 3			
	is the second number.					
	f =					
	h =					
2.	The first number times 5 is 3 less	В	f + 3h = 5			
	than the second number.					
	f =					
	h =					
3.	The sum of the first number and	С	3f + 5 = h			
	triple the second number is 5.					
	f =					
	h =					
4.	The quotient of the first number	D	$\frac{f}{5} = h - 3$			
	and 5 is equal to the difference					
	of the second number and 3.					
	f =					
	h = The Meadows Center for Preventing Educational Risk—Mat	nematics Instit	ute			

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Scoring Key: 1 point for defining each variable and Lesson 8: Variables as Quantities 1 point for each matching



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C

umulative Review Practice Score: ____ / 2 correct

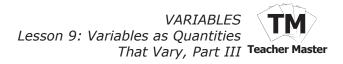
Read the following situations and select the equation that represents the relationship given in the word problem.

- 1. The sum of the first number and 15 is equal to the second number. (1 pt.)
 - f = the value of the first number. s = the value of the second number.

A 15 + s = f
B 15 + f = s
C s + f = 15
D 15 - f = s

- **2.** The product of the first number and 6 is equal to the difference of the second number and 2. (1 pt.)
 - f = the value of the first number. s = the value of the second number.

A 6 - s = 2f **B** 6 - f = 2s **C** 6f = s - 2**D** 6s = f - 2



C umulative Review Practice Key Score: / 2 correct

Read the following situations and select the equation that represents the relationship given in the word problem.

- **1.** The sum of the first number and 15 is equal to the second number. (1 pt.)
 - f = the value of the first number. s = the value of the second number.

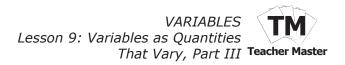
A
$$15 + s = f$$

B $15 + f = s$
C $s + f = 15$
D $15 - f = s$

- **2.** The product of the first number and 6 is equal to the difference of the second number and 2. (1 pt.)
 - f = the value of the first number. s = the value of the second number.

A
$$6 - s = 2f$$

B $6 - f = 2s$
C $6f = s - 2$
D $6s = f - 2$



Demonstration Practice

Independent and Dependent

When 2 quantities vary together, there is an independent variable and a dependent variable.

Independent Variable	Dependent Variable

Read the following situations and identify the 2 quantities that vary and the independent and dependent variables.

1. Every day I eat pizza in the cafeteria. The cost of my lunch varies, or changes based on how many slices of pizza I buy.

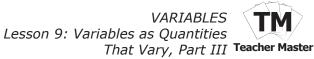
p = the number of slices of pizza I buy

c = the total cost of my lunch

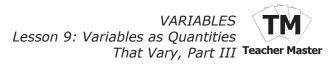
depends on

Independent variable

Dependent variable



Inat Vary, Part III Teacher Mas
D emonstration Practice (cont.)
2. Sandra has a job passing out flyers for a sandwich shop. The total
number of flyers that she passes out each day is determined by the
number of people that walk by her that day.
= the number of people that walk by
= the total number of flyers passed out
depends on
Independent variable
Dependent variable
3. Jonathan is trying to make money by washing cars in his neighborhood.
The number of cars that he washes will determine how much money that
he makes.
= the total amount of money made
= the number of cars washed
depends on
Independent variable
Dependent variable



Demonstration Practice Key

Independent and Dependent

When 2 quantities vary together, there is an independent variable and a dependent variable.

Independent Variable	Dependent Variable
The independent variable determines the value of the other variable. It does not depend on any other variable.	The dependent variable depends on the value of the other variable.

Read the following situations and identify the 2 quantities that vary and the independent and dependent variables.

1. Every day I eat pizza in the cafeteria. The cost of my lunch varies, or changes based on how many slices of pizza I buy.

p = the number of slices of pizza I buy

c = the total cost of my lunch

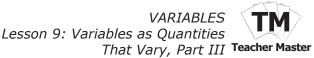
total cost of lunch

depends on

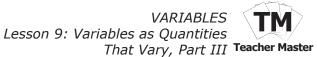
the number of pizza slices I buy.

Independent variable p = the number of slices of pizza.

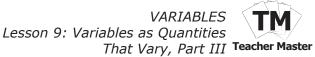
Dependent variable c = total cost of my lunch.

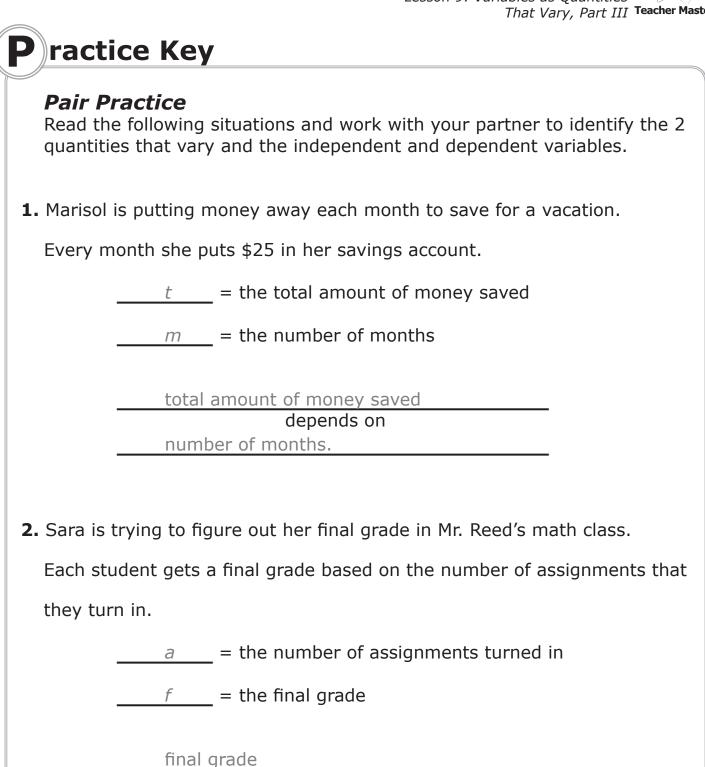


	Lesson 9: Variables as Quantities
(Demonstration Practice Key (cont.)
	2. Sandra has a job passing out flyers for a sandwich shop. The total
	number of flyers that she passes out each day is determined by the
	number of people that walk by her that day.
	p = the number of people that walk by
	f = the total number of flyers passed out
	total number of flyers passed out depends on
	the number of people that walk by.
	Independent variable $p =$ the number of people that walk by
	Dependent variable <u>f = the number of flyers passed out</u>
	3. Jonathan is trying to make money by washing cars in his neighborhood.
	The number of cars that he washes will determine how much money that
	he makes.
	<u>t</u> = the total amount of money made
	\underline{c} = the number of cars washed
	total amount of money made
	depends on number of cars washed.
	Independent variable <u>c = number of cars washed</u>
	Dependent variable $t = \text{total amount of money made}$



	Lesson 9: Variables as Quantities That Vary, Part III Teacher Ma
P ractice	
	tice owing situations and work with your partner to identify the 2 at vary and the independent and dependent variables.
1. Marisol is pu	itting money away each month to save for a vacation.
Every month	she puts \$25 in her savings account.
	= the total amount of money saved
	= the number of months
	depends on
2. Sara is tryin	g to figure out her final grade in Mr. Reed's math class.
Each studen	t gets a final grade based on the number of assignments that
they turn in.	
_	= the number of assignments turned in
	= the final grade
	depends on
-	
1	





depends on number of assignments turned in.

Name:

Independent Practice Score: / 12 correct
Read the following situations. Choose a variable to represent each quantity and label as independent or dependent. Each problem is worth 4 points.
1. Jose just got a summer job where the total amount of money he makes
each paycheck will be based on how many hours that he works.
= the number of hours that Jose works
= the amount of money Jose makes
2. Mark drives his car a lot for work and frequently needs to change the oil in his car. The number of oil changes that Mark's car needs each year is
determined by how many miles he drove that year.
= the number of oil changes Mark's car needs
= the number of miles driven
3. Angelica is having a party for her birthday. The number of people that
come to the party will determine how many pizzas that she will order.
= the number of pizzas that Angelica orders
= the number of people that come to the party

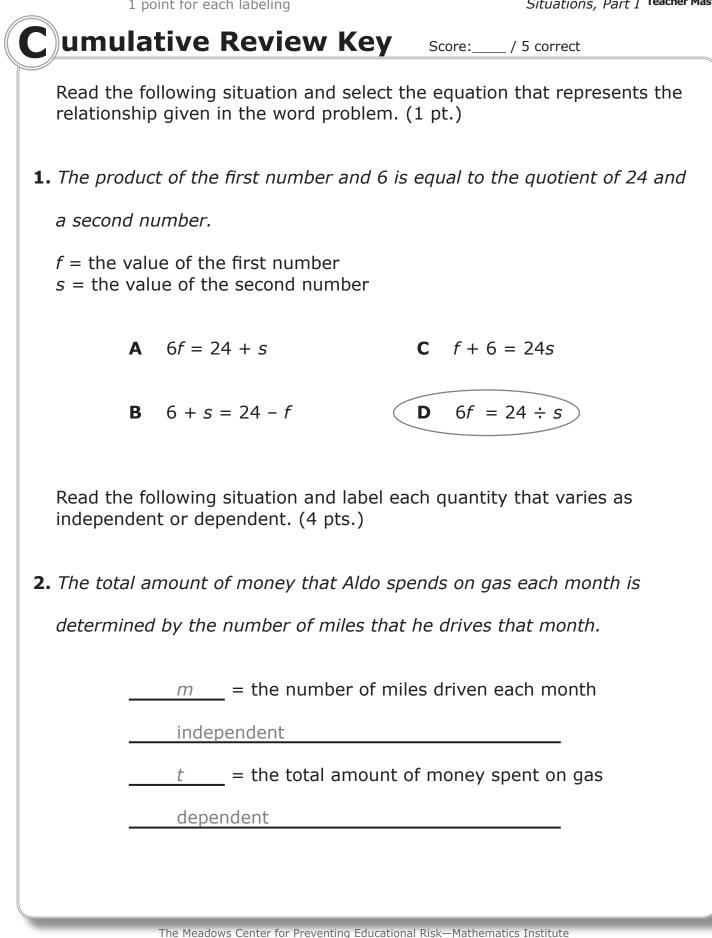
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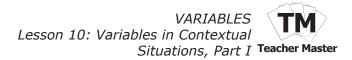
Scoring Key: 1 point for choosing a variable and 1 point for each labeling VARIABLES Lesson 9: Variables as Quantities That Vary, Part III Teacher Master		
Independent Practice Key Score:/ 12 correct		
Read the following situations. Choose a variable to represent each quantity and label as independent or dependent. Each problem is worth 4 points.		
1. Jose just got a summer job where the total amount of money he makes		
each paycheck will be based on how many hours that he works.		
h = the number of hours that Jose works		
independent		
p = the amount of money Jose makes		
dependent		
2. Mark drives his car a lot for work and frequently needs to change the oil		
in his car. The number of oil changes that Mark's car needs each year is		
determined by how many miles he drove that year.		
\underline{c} = the number of oil changes Mark's car needs		
dependent		
= the number of miles driven		
independent		
3. Angelica is having a party for her birthday. The number of people that		
come to the party will determine how many pizzas that she will order.		
p = the number of pizzas that Angelica orders		
dependent		
\underline{t} = the number of people that come to the party		
independent		



umulative Review Score: / 5 correct Read the following situation and select the equation that represents the relationship given in the word problem. (1 pt.) **1.** The product of the first number and 6 is equal to the quotient of 24 and a second number. f = the value of the first number s = the value of the second number **C** f + 6 = 24s**A** 6f = 24 + s6 + s = 24 - f**D** $6f = 24 \div s$ R Read the following situation and label each quantity that varies as independent or dependent. (4 pts.) 2. The total amount of money that Aldo spends on gas each month is determined by the number of miles that he drives that month. = the number of miles driven each month = the total amount of money spent on gas

Scoring Key: 1 point for choosing a variable and Lesson 10: Variables in Contextual 1 point for each labeling







D emonstration Practice

1. Word Problem:	Define Variable(s):	
Alicia works at an electronic	Let the variable	
store where she makes \$11	stand for	
each hour.		
Find the total amount of		
money Alicia makes.	Let the variable	
	stand for	
Write an Equation:		
Write an equation that can be used to find the total amount of money that Alicia makes based on how many hours that she works.		
Calculate the money earned	Total money made	
	=	



|--|

2. Word Problem:	Define Variable(s):	
The total cost of shipping a	Let the variable	
package is \$2 per pound.	stand for	
Find the total cost of		
shipping a package.		
	Let the variablestand for	
Write an Equation:		
Write an equation that can be used to find the total cost of a package based on its weight.		
Calculate the package shipping cost	=	





Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):		
Stephen is saving up to	Let the variable		
buy a car. He is putting \$40	stand for		
per month in his savings			
account. Find the total			
amount Stephen has saved.	Let the variable		
	stand for		
Write an Equation:			
Write an equation that can be used to find the total amount of money that Stephen saves based on the number of months he has saved for.			
Calculate the savings	=		





D emonstration Practice Key

1. Word Problem:	Define Variable(s):		
Alicia works at an electronic store where she makes \$11 each hour. Find the total amount of money Alicia makes.	Let the variable t stand for total amount of money that Alicia makes. Let the variable h stand for number of hours Alicia works.		
Write an Equation:			
Write an equation that can be used to find the total amount of money that Alicia makes based on how many hours that she works.			
Calculate the money earned 11h	= Total money made t		

VARIABLES Lesson 10: Variables in Contextual Situations, Part I Teacher Master



D emonstration Practice Key (cont.)

2. Word Problem:	Define Variable(s):	
The total cost of shipping a package is \$2 per pound. Find the total cost of shipping a package.	Let the variable <u>t</u> stand for <u>total cost of</u> <u>shipping the package.</u>	
	Let the variable <u>w</u> stand for <u>weight of the</u> <u>package in pounds.</u>	
Write an Equation:		
Write an equation that can be used to find the total cost of a package based on its weight.		
Calculate the package shipping cost	= <u>Total cost</u>	

VARIABLES Lesson 10: Variables in Contextual Situations, Part I Teacher Master



D emonstration Practice Key (cont.)

3. Word Problem:	Define Variable(s):
Stephen is saving up to buy a car. He is putting \$40 per month in his savings account. Find the total amount Stephen has saved.	Let the variable stand for money saved. Let the variable stand for the number of months.
· ·	ed to find the total amount of money number of months he has saved for. = <u>Total savings</u> <u>t</u>



Pair Practice

For each of the following situations, work with your partner to define the variables and write the equation to represent the situation.

Jorge went to the carnival with his friend. The carnival charges \$3 per

ride. Jorge needs to figure out how much money he will spend at the

carnival based on the number of rides he takes.

1. Determine and define the variables:

Let the variable	

stand for	

Let the variable _____

2. Based on the variables you defined above, write an equation to represent the carnival situation above.

=

Calculate the ride cost

Total Carnival cost



P ractice Key

Pair Practice

For each of the following situations, work with your partner to define the variables and write the equation to represent the situation.

Jorge went to the carnival with his friend. The carnival charges \$3 per

ride. Jorge needs to figure out how much money he will spend at the

carnival based on the number of rides he takes.

1. Determine and define the variables:

Let the v	ariable	r

stand for the number of rides

Let the variable _____ m___

stand for amount of money spent

2. Based on the variables you defined above, write an equation to represent the carnival situation above.

Calculate the ride cost		<u>Total Carnival cost</u>
3 <i>r</i>	=	m

VARIABLES Lesson 10: Variables in Contextual Situations, Part I Teacher Master

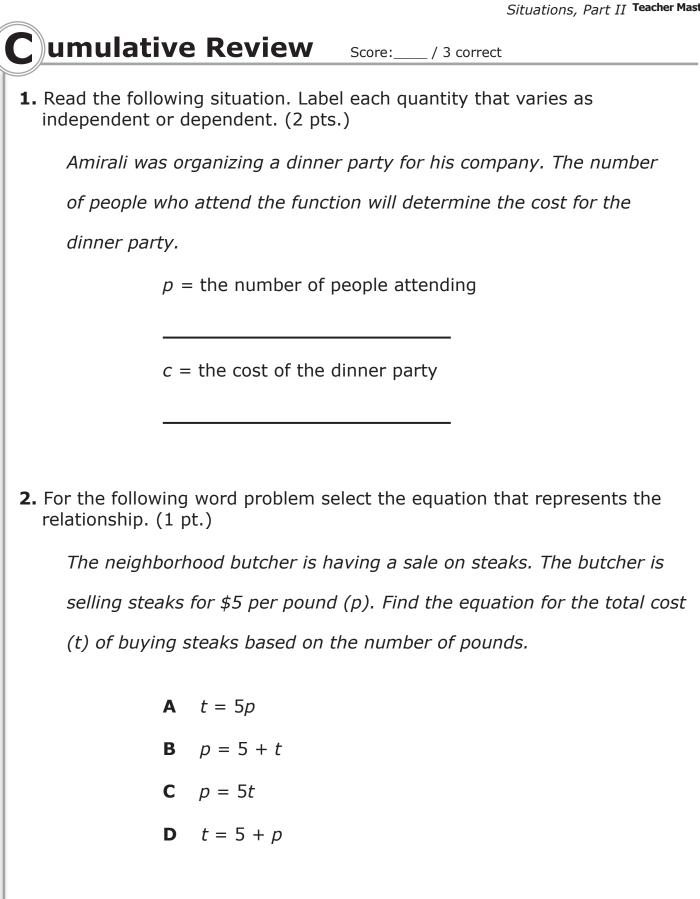


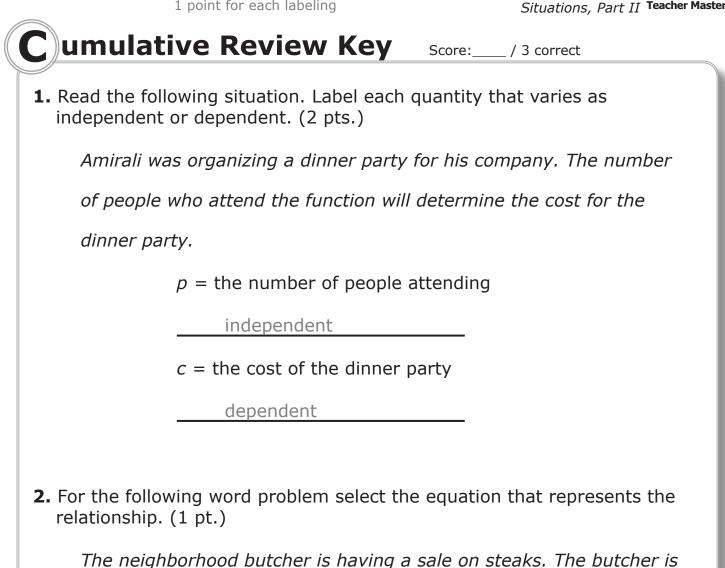
Name: _____

(Independent Practice Score: / 4 correct
	Read the following word problems and find the matching equation that represents the relationship. Each match is worth 1 point.
	1. Sally works at a cell phone store where
	she earns \$15 commission for every cell
	phone (c) that she sells. Find the equation
	for the total (t) money made. $A = 3c$
	2. The cost (<i>c</i>) of the membership to a gym
	is \$15 per month (t). Find the equation for
	the total cost for t months. $\qquad \qquad \qquad$
	3. A DVD club charges \$3 per DVD (c). Find
	the equation for the total (t) cost of the
	DVD club per month. $\qquad \qquad \qquad$
	4. The cost (<i>c</i>) of renting a canoe is \$3 per
	hour (t). Find the equation for the total
	cost for renting a canoe t hours. $D t = 15c$

VARIABLES Lesson 10: Variables in Contextual Situations, Part I Teacher Master

	Situations, Part I Teacher Maste
Independent Practice Key Score	:/ 4 correct
Read the following word problems and find the mare represents the relationship. Each match is worth a	
1. Sally works at a cell phone store where	
she earns \$15 commission for every cell	
phone (c) that she sells. Find the equation	
for the total (t) money made. D	A $t = 3c$
2. The cost (<i>c</i>) of the membership to a gym	
is \$15 per month (t). Find the equation for	
the total cost for <i>t</i> months.	B <i>c</i> = 3 <i>t</i>
3. A DVD club charges \$3 per DVD (c). Find	
the equation for the total (t) cost of the	
DVD club per month.	C $c = 15t$
4. The cost (<i>c</i>) of renting a canoe is \$3 per	
hour (t) . Find the equation for the total	
cost for renting a canoe <i>t</i> hours.	D $t = 15c$



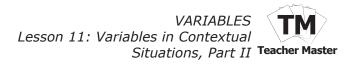


selling steaks for \$5 per pound (p). Find the equation for the total cost

(*t*) of buying steaks based on the number of pounds.

A
$$t = 5p$$

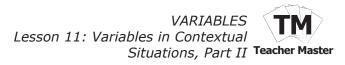
B $p = 5 + t$
C $p = 5t$
D $t = 5 + p$



D emonstration Practice

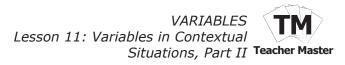
For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):
Midori is saving up to buy	Let the variable
a car. Her account has an	stand for
initial balance of \$300 and	
she is depositing \$40 per	
month into her account. Find	Let the variable
an equation to represent the	stand for
amount Midori has saved.	
Write an Equation:	Make a Table:
Write an equation that can be used to find the balance in Midori's account based on how long she has saved.	Use the table to find out how much money Midori has saved for the different number of months.
Amount Initial Total Deposited + Balance = + = Initial	



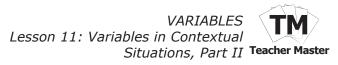
Demonstration Practice (cont.)

2. Word Problem:	Define Variable(s):
The cost of a taxi ride in Chicago is \$0.50 per mile plus an additional fee of \$5.	Let the variable stand for
Find the total cost of a taxi ride.	Let the variable stand for
Write an Equation:	Make a Table:
Write an equation that can be used to find the total cost of a taxi ride based on the distance traveled. $\begin{bmatrix} Total \\ Cost \end{bmatrix} = \begin{bmatrix} Cost of \\ Miles \\ + \end{bmatrix} + \begin{bmatrix} Initial \\ Fee \\ \end{bmatrix}$	Use the table to find out how much a taxi ride costs for different distances traveled.



Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):	
Johanna is planning a trip and will rent a car. The cost of renting a car is \$10 per	Let the variable stand for	
day plus the initial fee of \$25. Find the total cost of a rental car.	Let the variable stand for	
Write an Equation:	Make a Table:	
Write an equation that can be used to find the total rental cost based on how long Johanna rents the car. Cost of Initial Total Pee Fee $Cost$ $+$ $=$ $Cost$	Use the table to find out the total cost for different number of days.	



D emonstration Practice Key

For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):		
Midori is saving up to buy	Let the variable <u>m</u>		
a car. Her account has an	stand for the number of		
initial balance of \$300 and	months saving.		
she is depositing \$40 per			
month into her account. Find	Let the variable <u>t</u>		
an equation to represent the	stand for the total amount of		
amount Midori has saved.	money saved.		
Write an Equation:	Make a Table:		
Write an equation that can be used to find the balance in Midori's account based on how long she has saved.	Use the table to find out how much money Midori has saved for the different number of months.		
Amount Initial Total	m Process t		
Deposited Balance Saved	2 40(2)+300 380 3 40(3)+300 420		
40m + 300 = t	3 40(3)+300 420 4 40(4)+300 460		
(answers may vary)			

VARIABLES Lesson 11: Variables in Contextual Situations, Part II Teacher Master



D emonstration Practice Key (cont.)

	1	
2. Word Problem:	Define Variable(s):	
The cost of a taxi ride in Chicago is \$0.50 per mile plus an additional fee of \$5.	Let the variable <u>t</u> stand for <u>the total cost</u> <u>of taxi ride.</u>	
Find the total cost of a taxi ride.	Let the variable <u>m</u> stand for <u>the number of</u> <u>miles driven.</u>	
Write an Equation:	Make a Table:	
Write an equation that can be used to find the total cost of a taxi ride based on the distance traveled.	Use the table to find out how much a taxi ride costs for different distances traveled.	
Total CostCost of MilesInitial Feet=0.50m+	mProcesst1 $0.50(1)+5$ 5.50 2 $0.50(2)+5$ 63 $0.50(3)+5$ 6.50	
	(answers may vary)	

VARIABLES Lesson 11: Variables in Contextual Situations, Part II Teacher Master



Demonstration Practice Key (cont.)

3. Word Problem:	Define Variable(s):		
Johanna is planning a trip	Let the variable <u>d</u>		
and will rent a car. The cost	stand for the number of days		
of renting a car is \$10 per	renting a car.		
day plus the initial fee of	Let the variable <u>t</u>		
\$25. Find the total cost of	stand for total cost of		
a rental car.	renting the car.		
Write an Equation:	Make a Table:		
Write an equation that can be used to find the total rental cost based on how long Johanna rents the car.	Use the table to find out the total cost for different number of days.		
Cost ofInitialTotalDaysFeeCost	d Process t		
	1 10(1)+25 35		
10 <i>d</i> 25 <i>t</i>	2 10(2)+25 45		
+ =	3 10(3)+25 55		
	(answers may vary)		

P ractice

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

Peter signed up for a new cell phone plan. His plan each month will

cost him \$35 plus \$0.10 per minute.

Define and describe variables to represent each of the unknown values:

1. The equation that represents the situation is:

A c = 0.10m + 35 **C** m = 0.10c + 35

B c = 35.10m **D** c + 35 = 0.10m

2. The table that represents the situation is:

A Number of minutes (<i>m</i>)		Total phone bill cost (c)	С	Number o minutes (<i>r</i>
	20	55		55
	50	85		85
	100	135		135

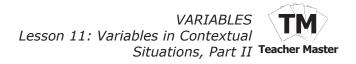
Number of minutes (m)	Total phone bill cost (c)	
55	20	
85	50	
135	100	

1	
	Б.
	-

Number of minutes (<i>m</i>)	Total phone bill cost (<i>c</i>)
37	20
40	50
45	100

Number of minutes (m)	Total phone bill cost (c)	
20	37	
50	40	
100	45	

D



P ractice Key

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

Peter signed up for a new cell phone plan. His plan each month will

cost him \$35 plus \$0.10 per minute.

Define and describe variables to represent each of the unknown values:

m = the number of minutes used.

c = the cost of his plan each month.

1. The equation that represents the situation is:

A c = 0.10m + 35 **C** m = 0.10c + 35

B c = 35.10m **D** c + 35 = 0.10m

2. The table that represents the situation is:

Α	Number of minutes (m)		С	Number of minutes (m)	Total phone bill cost (<i>c</i>)
	20	55		55	20
	50	85		85	50
	100	135		135	100

В	Number of minutes (m)	Total phone bill cost (c)	D	Nur mint
	37	20		
	40	50		
	45	100		
		•		

/	Number of minutes (<i>m</i>)	Total phone bill cost (c)	
	20	37	
	50	40	
	100	45	

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rror Correction Practice

Ε

The given situation is work completed by a student. Determine the error in the students work and explain your reasoning.

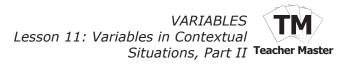
For the given situation, write the equation and complete a table.

Isabella rented a motor scooter for the day. To rent a scooter,

it costs \$20 plus an additional \$10 an hour.

c = 10 + 20h

Hours Rented (<i>h</i>)	Total Cost (<i>c</i>)
1	30
2	50
3	70



E rror Correction Practice Key

The given situation is work completed by a student. Determine the error in the students work and explain your reasoning.

For the given situation, write the equation and complete a table.

Isabella rented a motor scooter for the day. To rent a scooter,

it costs \$20 plus an additional \$10 an hour.

Hours
Rented
(h)Total
Cost
(c)130250370

c = 10 + 20h

The equation is wrong. It should be

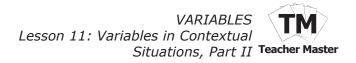
c = 10h + 20. The unit rate is \$10 an hour,

therefore \$10 is multiplied by the number of

hours. The table is also wrong. The cost of

renting for 2 hours should be \$40 and the cost

of renting for 3 hours should be \$50.



Name:

Independent Practice Score:___/ 2 correct

For the following situation, circle the correct equation and table representation.

George signed up for a new cable plan. Each month, he is charged a

\$50 fee, plus \$5 per movie package. Find George's total cost for cable.

С

1. The equation that represents the situation is: (1 pt.)

A c = m + 50 **C** c = 50m**B** c = 5m + 50 **D** c = 50m + 5

2. The table that represents the situation is: (1 pt.)

Α	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	50
	2	55
	3	60

Movie packages(<i>m</i>)	cost (<i>c</i>)
1	55
2	60
3	65

B	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	50
	2	100
	3	150

D	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	5
	2	55
	3	105

VARIABLES Lesson 11: Variables in Contextual Situations, Part II Teacher Master



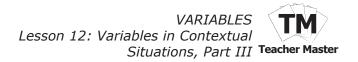
I ndependent Practice Key Score:____ / 2 correct For the following situation, circle the correct equation and table representation. George signed up for a new cable plan. Each month, he is charged a \$50 fee, plus \$5 per movie package. Find George's total cost for cable. **1.** The equation that represents the situation is: (1 pt.) c = m + 50c = 50mΑ С c = 5m + 50c = 50m + 5B D **2.** The table that represents the situation is: (1 pt.) Α

Movie packages(m)	cost (<i>c</i>)
1	50
2	55
3	60

C	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	55
	2	60
	3	65

B	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	50
	2	100
	3	150

D	Movie packages(<i>m</i>)	cost (<i>c</i>)
	1	5
	2	55
	3	105



umulative Review Score: / 3 correct **1.** Read the following word problem and select the equation that represents the relationship. (1 pt.) The cost (c) of renting a bike to tour downtown is \$15 per hour (h). Find the equation for the total cost for renting a bike. c = h + 15h = 15cΑ С h = c + 15R D c = 15hUse the following word problem to answer questions 2 and 3. Nikita is planning the company summer party. The party will cost (*c*) \$6 per person (p) plus a rental fee of \$65 for setup services.

2. Select the equation that represents the word problem. (1 pt.)

A c = 65p + 6 **B** c = 6p + 65 **C** c = p + 65**D** c = p + 6

3. Select the table that represents the word problem. (1 pt.)

Α	Number of People (<i>p</i>)	Total Cost (<i>c</i>)
	1	71
	2	77
	3	83

Number of People (<i>p</i>)	Total Cost (<i>c</i>)
1	65
2	71
3	77

В	Number of People (<i>p</i>)	Total Cost (<i>c</i>)	D	Number of People (<i>p</i>)	Total Cost (<i>c</i>)
	1	71		1	66
	2	136		2	67
	3	201		3	68

С

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C umulative Review Key Score: / 3 correct

1. Read the following word problem and select the equation that represents the relationship. (1 pt.)

The cost (c) of renting a bike to tour downtown is \$15 per hour (h).

Find the equation for the total cost for renting a bike.

A
$$c = h + 15$$

B $h = c + 15$
C $h = 15c$
D $c = 15h$

Use the following word problem to answer questions 2 and 3.

Nikita is planning the company summer party. The party will cost (c)

\$6 per person (p) plus a rental fee of \$65 for setup services.

2. Select the equation that represents the word problem. (1 pt.)

A
$$c = 65p + 6$$

B $c = 6p + 65$
C $c = p + 65$
D $c = p + 6$

3. Select the table that represents the word problem. (1 pt.)

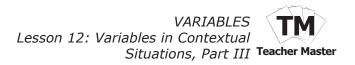
A	Number of People (<i>p</i>)	Total Cost (<i>c</i>)
(1	71
	2	77
	3	83

Number of People (<i>p</i>)	Total Cost (<i>c</i>)
1	65
2	71
3	77

В	Number of People (<i>p</i>)	Total Cost (<i>c</i>)	D	Number of People (<i>p</i>)	Total Cost (<i>c</i>)
	1	71		1	66
	2	136		2	67
	3	201		3	68

С

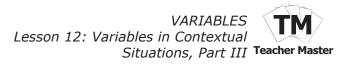
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D emonstration Practice

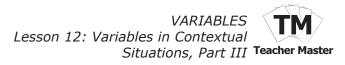
For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):
Margret is selling cups of lemonade to earn money. She already has \$5 and is selling the lemonade for \$1.50 per cup. Find the total amount of money Margret has.	Let the variable stand for Let the variable stand for
Write an Equation:	Make a Table:
Write an equation that can be used to find Margret's total amount of money based on the number of cups of lemonade she has sold.	Use the table to calculate the varying amount of money Margret made for your selected numbers of cups of lemonade sold.



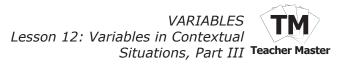
Demonstration Practice (cont.)

2. Word Problem:	Define Variable(s):
Lilia wants to rent a motor scooter. To rent a scooter it costs \$0.30 per mile, plus an initial fee of \$45. Find the total cost to rent a scooter.	Let the variable stand for Let the variable stand for
Write an Equation:	Make a Table:
Write an equation that can be used to find the total cost of renting a motor scooter based on the number of miles driven.	Use the table to calculate the varying costs to rent a scooter for your selected numbers of miles driven.



Demonstration Practice (cont.)

3. Word Problem:	Define Variable(s):	
Lorenzo joined a soccer	Let the variablestand for	
league for \$20. Lorenzo pays \$5 for each game he plays.		
Find the total cost to play on	Let the variable stand for	
the soccer league.	Maka a Tablar	
Write an Equation:	Make a Table:	
Write an equation that can be used to find the total cost for Lorenzo to play soccer based on the number of games he plays.	Use the table to calculate the varying total costs for the league for your selected numbers of soccer games played.	
	Process	



D emonstration Practice Key

For each of the following situations, define and describe the variables, create an equation and a table representation.

1. Word Problem:	Define Variable(s):	
Margret is selling cups of	Let the variable <u>c</u>	
lemonade to earn money.	stand for	
She already has \$5 and is	the number of cups sold.	
selling the lemonade for		
\$1.50 per cup.	Let the variable <u>t</u>	
Find the total amount of	stand for	
money Margret has.	the total amount of money.	
Write an Equation:	Make a Table:	
Write an equation that can be used to find Margret's total amount of money based on the number of cups of lemonade she has sold.	Use the table to calculate the varying amount of money Margret made for your selected numbers of cups of lemonade sold.	
	c Process t	
	21.50(2)+58.0031.50(3)+59.50	
	4 1.50(4)+5 11.00	
1.50 c + 5 = t	(answers may vary)	

VARIABLES Lesson 12: Variables in Contextual Situations, Part III Teacher Master



D emonstration Practice Key (cont.)

2. Word Problem:	Define Variable(s):	
Lilia wants to rent a motor	Let the variable <u>t</u>	
scooter. To rent a scooter it	stand for <u>the total</u> cost of the rental.	
costs \$0.30 per mile, plus		
an initial fee of \$45. Find the	Let the variable <u>m</u>	
total cost to rent a scooter.	stand for <u>the number</u> of miles driven.	
Write an Equation:	Make a Table:	
Write an equation that can be used to find the total cost of renting a motor scooter based on the number of miles driven.	Use the table to calculate the varying costs to rent a scooter for your selected numbers of miles driven.	
<i>t</i> = .30 <i>m</i> + 45	m Process t 5 .30(5)+45 46.50 10 .30(10)+45 47.00 20 .30(20)+45 51.00	

VARIABLES Lesson 12: Variables in Contextual Situations, Part III Teacher Master



D emonstration Practice Key (cont.)

3. Word Problem:	Define Variable(s):	
Lorenzo joined a soccer	Let the variableg	
league for \$20. Lorenzo pays	stand for the number of games played.	
\$5 for each game he plays.		
Find the total cost to play on	Let the variable <u>t</u>	
the soccer league.	stand for <u>the total cost</u> of the soccer league.	
Write an Equation:	Make a Table:	
Write an equation that can be used to find the total cost for Lorenzo to play soccer based on the number of games he plays.	Use the table to calculate the varying total costs for the league for your selected numbers of soccer games played.	
	g Process t 5 5(5)+20 45	
t = 5g + 20	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	(answers may vary)	

Practice

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

At a local copy shop, it costs \$0.50 per page of colored copy plus an

initial processing fee of \$4. Find the cost of making color copies.

Define and describe variables to represent each of the unknown values:

1. The equation that represents the situation is:

A p = 0.50c + 5 **C** c = 0.50p + 4

B c + 4 = 0.50p **D** c = 4.50p

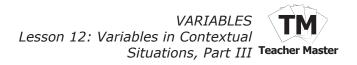
2. The table that represents the situation is:

Α	Number of Pages (p)	Total Copy Cost (<i>c</i>)	C
	5	2	
	7	6	
	9	10	

Number of Pages (p)	Total Copy Cost (c)
2	9
6	27
10	45

В	

Number of Pages (<i>p</i>)	Total Copy Cost (<i>c</i>)	D	Number of Pages (p)	Total Copy Cost (c)
2	5		2	4.50
6	7		6	5.50
10	9		10	8



P ractice Key

Α

Pair Practice

With a partner, define and describe the variables, circle the letter for the correct equation and table representation.

At a local copy shop, it costs \$0.50 per page of colored copy plus an

initial processing fee of \$4. Find the cost of making color copies.

Define and describe variables to represent each of the unknown values:

c = the cost of the copies

p = the the number of pages

1. The equation that represents the situation is:

A
$$p = 0.50c + 5$$
 C $c = 0.50p + 4$

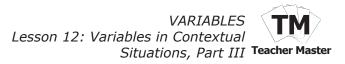
B c + 4 = 0.50p **D** c = 4.50p

2. The table that represents the situation is:

Number of Pages (<i>p</i>)	Total Copy Cost (<i>c</i>)	C	Number of Pages (<i>p</i>)	Total Copy Cost (c)	
5	2		2	9	
7	6		6	27	
9	10		10	45	
9	10		10	45	

_			_		
В	Number of Pages (p)	Total Copy Cost (<i>c</i>)	D	Number of Pages (p)	Total Copy Cost (<i>c</i>)
	2	5)	2	4.50
	6	7		6	5.50
	10	9		10	8

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E rror Correction Practice

The given situations are work completed by two different students. Determine which student is incorrect and explain the error(s).

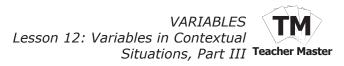
Given the following contextual situation, write an equation to describe the relationship between the quantities that vary.

Marie and Joanna are renting a canoe. The canoe rental costs a flat fee of

\$7 plus \$5 per hour (h). Find the equation for the total cost (c).

Student 1: Student 2:

7h + 5 = c 7 + 5h = c



E rror Correction Practice Key

The given situations are work completed by two different students. Determine which student is incorrect and explain the error(s).

Given the following contextual situation, write an equation to describe the relationship between the quantities that vary.

Marie and Joanna are renting a canoe. The canoe rental costs a flat fee of

\$7 plus \$5 per hour (h). Find the equation for the total cost (c).

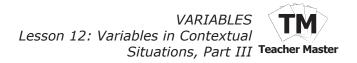
Student 1:	Student 2:
------------	------------

7h + 5 = c 7 + 5h = c

Student 1 was incorrect because \$5 per hour

should be 5h and a flat fee is +7,

so the equation should be 7 + 5h = c.



Name:

ndependent Practice Score:___ / 2 correct

For the following situation, circle the correct equation and table representation.

Amir is purchasing a pizza from a local shop. The pizza costs \$12 plus

С

D

\$0.50 for each topping. Find the cost of a pizza.

1. The correct equation is: (1 pt.)

c = t + 12С c = 12.50tΑ c = 12t + 0.50**D** c = 0.50t + 12B

2. The correct table is: (1 pt.)

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	13.50
2	14.00
3	14.50

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	12.50
2	13.00
3	13.50

В

Α

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	12.00
2	13.00
3	14.00

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	12.50
2	24.00
3	36.50

VARIABLES Lesson 12: Variables in Contextual Situations, Part III Teacher Master

I ndependent Practice Key Score:____ / 2 correct

For the following situation, circle the correct equation and table representation.

Amir is purchasing a pizza from a local shop. The pizza costs \$12 plus

\$0.50 for each topping. Find the cost of a pizza.

1. The correct equation is: (1 pt.)

A c = t + 12 **B** c = 12t + 0.50 **C** c = 12.50t**D** c = 0.50t + 12

2. The correct table is: (1 pt.)

Α

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	13.50
2	14.00
3	14.50

~		
C	Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
(1	12.50
	2	13.00
	3	13.50

B	Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
	1	12.00
	2	13.00
	3	14.00

Number of Toppings (<i>t</i>)	Cost of a Pizza (<i>c</i>)
1	12.50
2	24.00
3	36.50

D